

Magnetar QPOs and perspective with LOFT

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Outline

- Introduction
- Models
- Superfluid cores
- Conclusions

Introduction

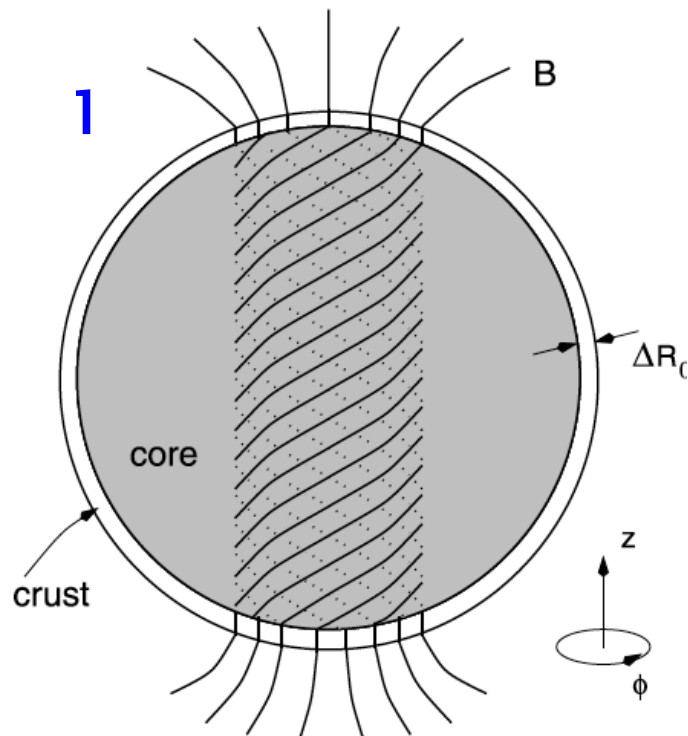
Soft Gamma Repeaters (SGRs)

Observations

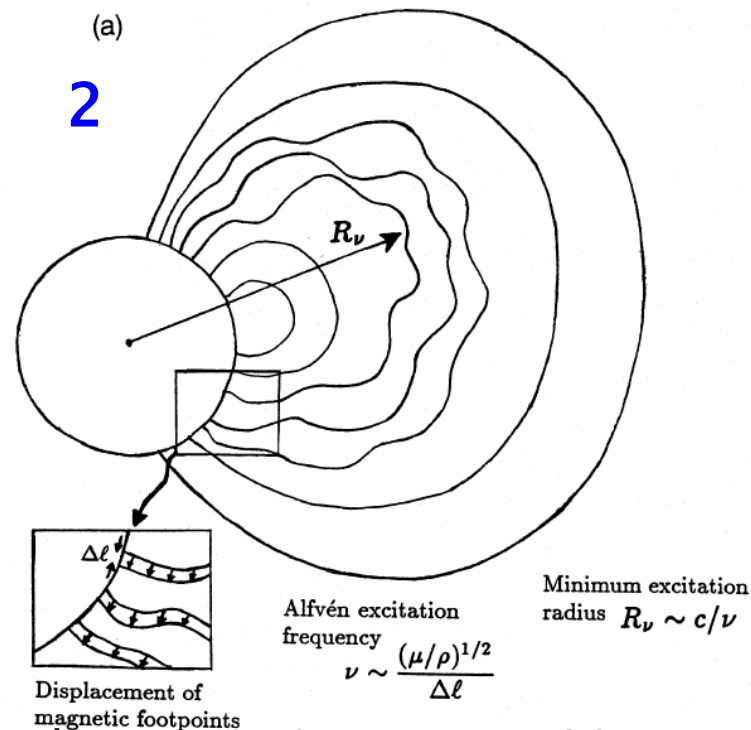
- Recurrent gamma-ray flare activity
- Nearby (Galactic or LMC)
- Associated to SNR
- Slowly rotating ($P \sim 5-10$ s)
- Rapid spin down (Kouveliotou et al 1998)

Model

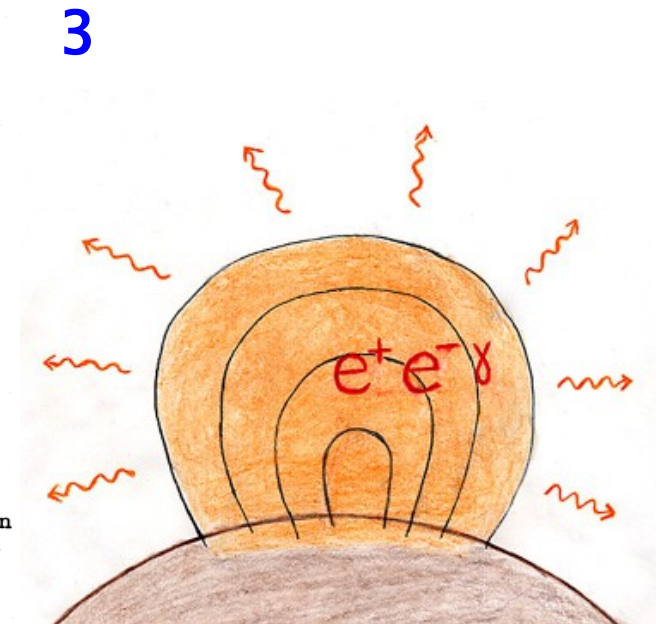
- Strongly magnetized NS : magnetar (Duncan & Thompson 1992)
- $B > 10^{14}$ G
- **1** : Stresses build in the crust
- **2** : Crust breaks and releases energy
- **3** : Fireball and x-ray emission



Thompson & Duncan 2001



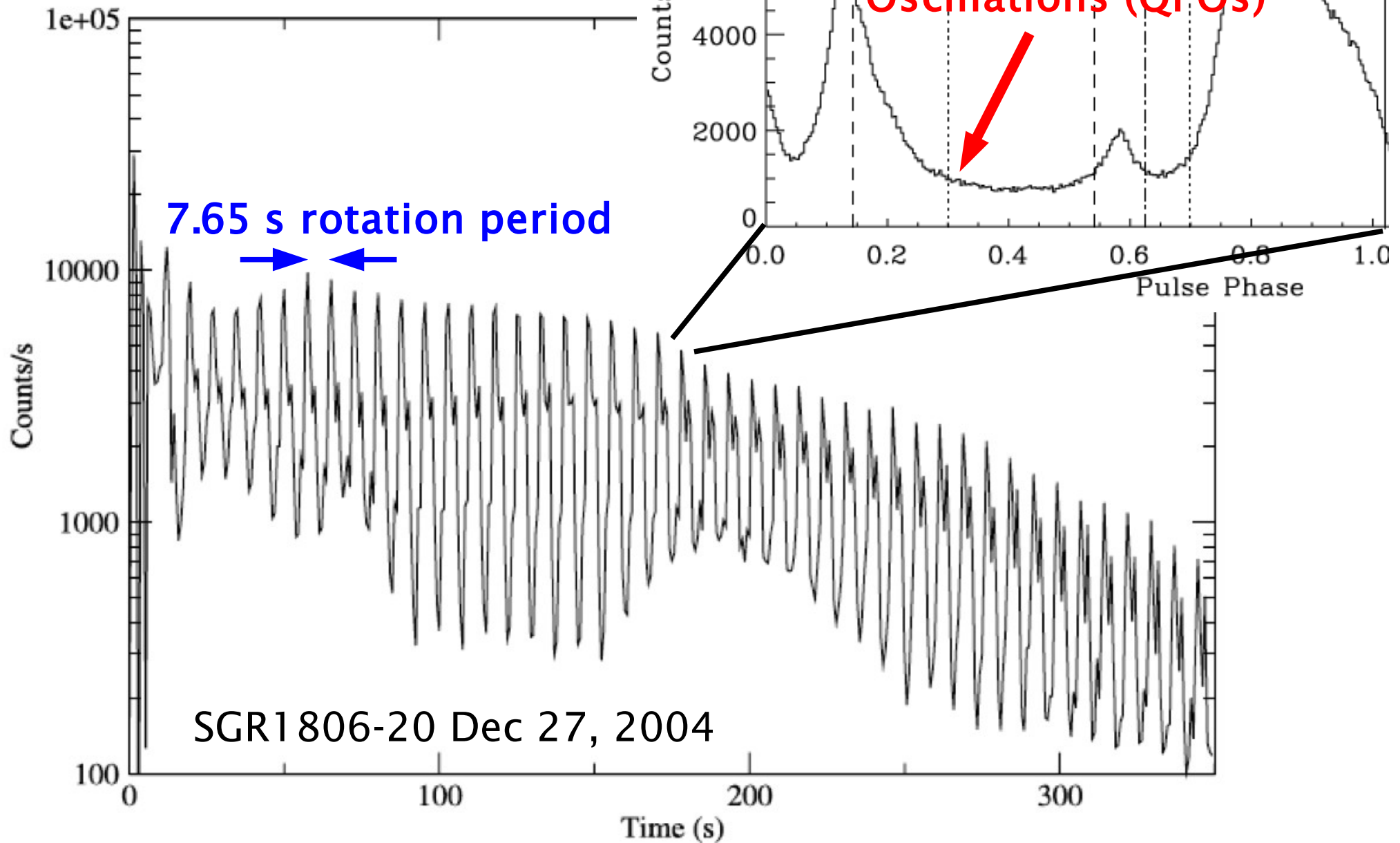
Thompson & Duncan 1995



R.C. Duncan

QPOs in giant flares

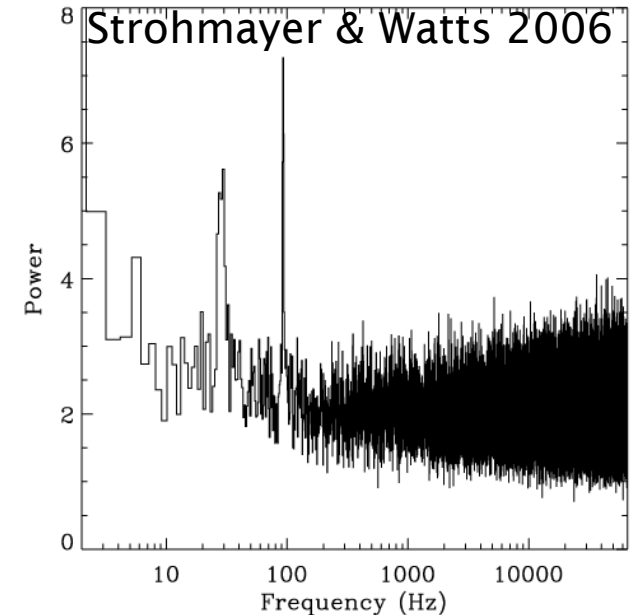
X-ray tail (~ 100 s)



Strohmayer & Watts
2006

QPOs in giant flares

- SGR 0526-66 on March 5, 1979 :
→ 43 Hz ? (Barat et al 1983)
- SGR 1900+14 on Aug. 27, 1998 :
→ 28, 56, 84, 155 Hz (Strohmayer & Watts 2005)
- SGR 1806-20 on Dec 27, 2004 :
→ 18, 26, 30, 92, 150, 625, 1840 Hz
(Israel et al 2005; Watts & Strohmayer 2006, Strohmayer & Watts 2006)



+ Two frequency bands:

- Low frequency QPOs : 17 → 155 Hz
- High frequency QPOs: 625 → 1840 Hz

+ Rotational phase dependence: origin close to the star

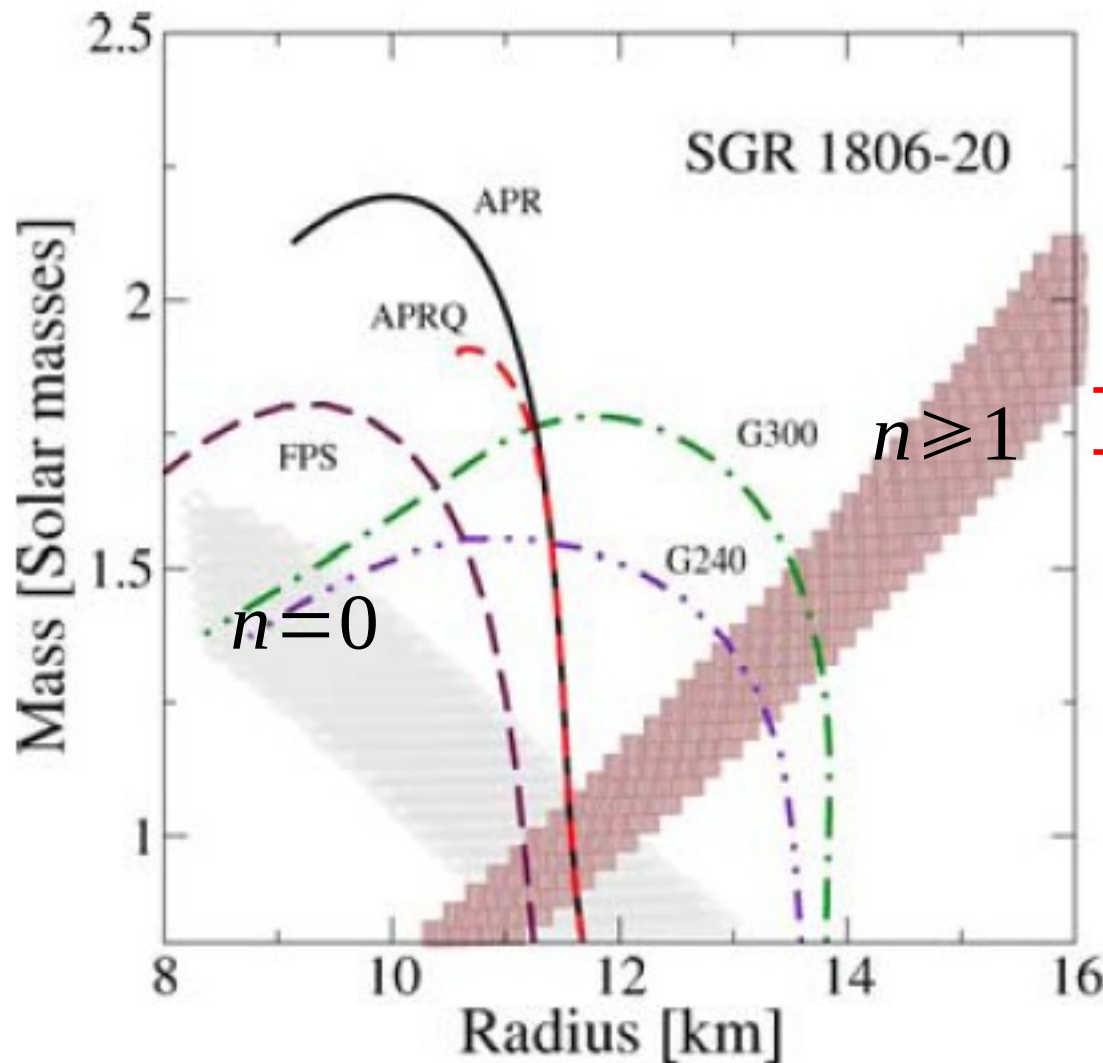
+ Variability (frequency and amplitude)

+ Large uncertainties bellow 30 Hz (Huppenkothen et al 2013)

Models

Crust shear oscillations model

(Schomaker & Thorne 1983, Piro 2005, Samuelsson & Andersson 2007)

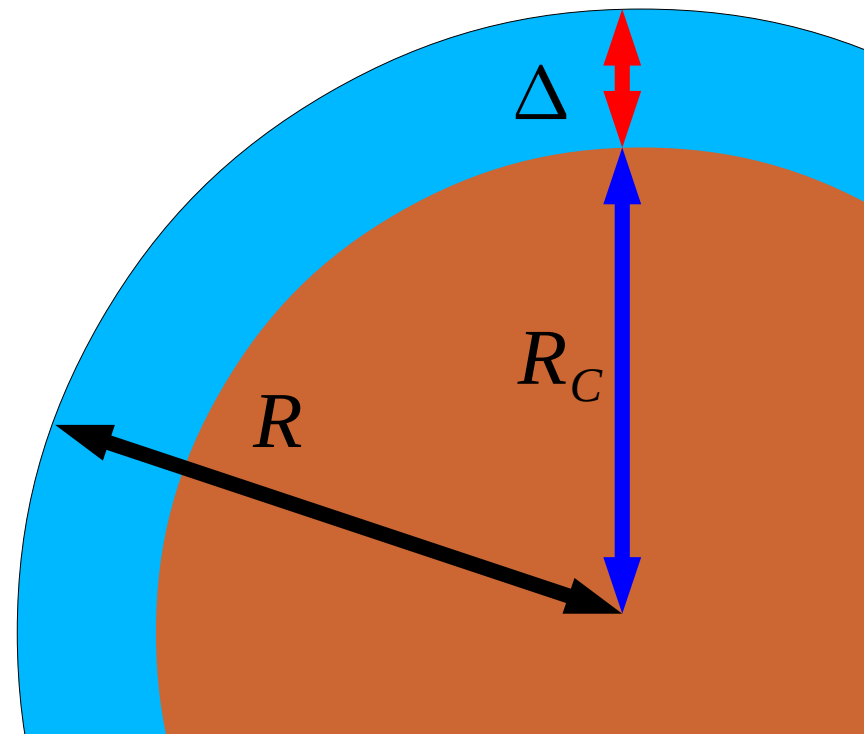


Samuelsson & Andersson 2007

$$\omega^2 \approx \frac{v_t^2 (l-1)(l+2)}{R R_C} \quad n=0$$

$$\omega \approx \frac{n \pi v_r}{\Delta} \quad n \geq 1$$

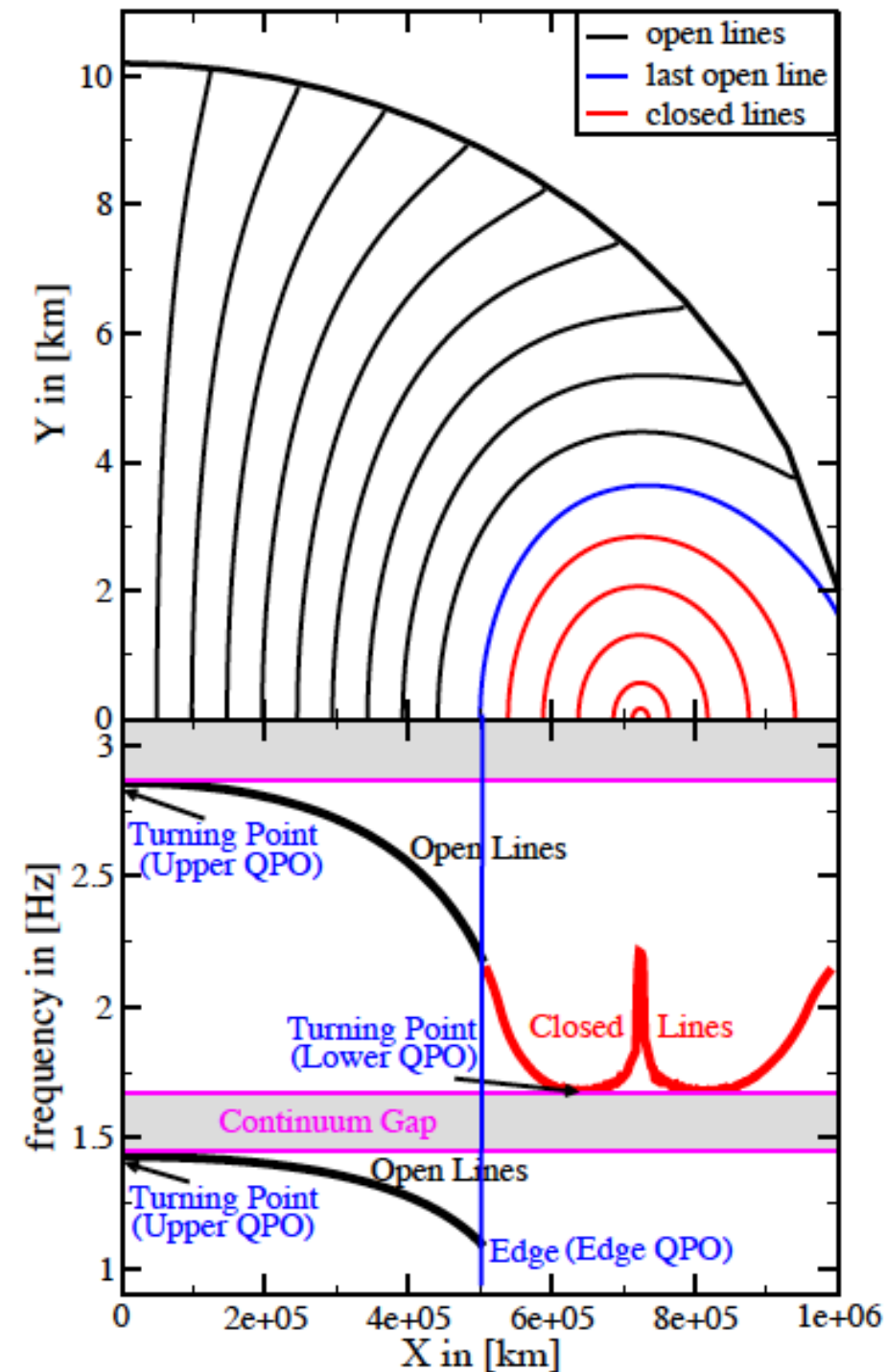
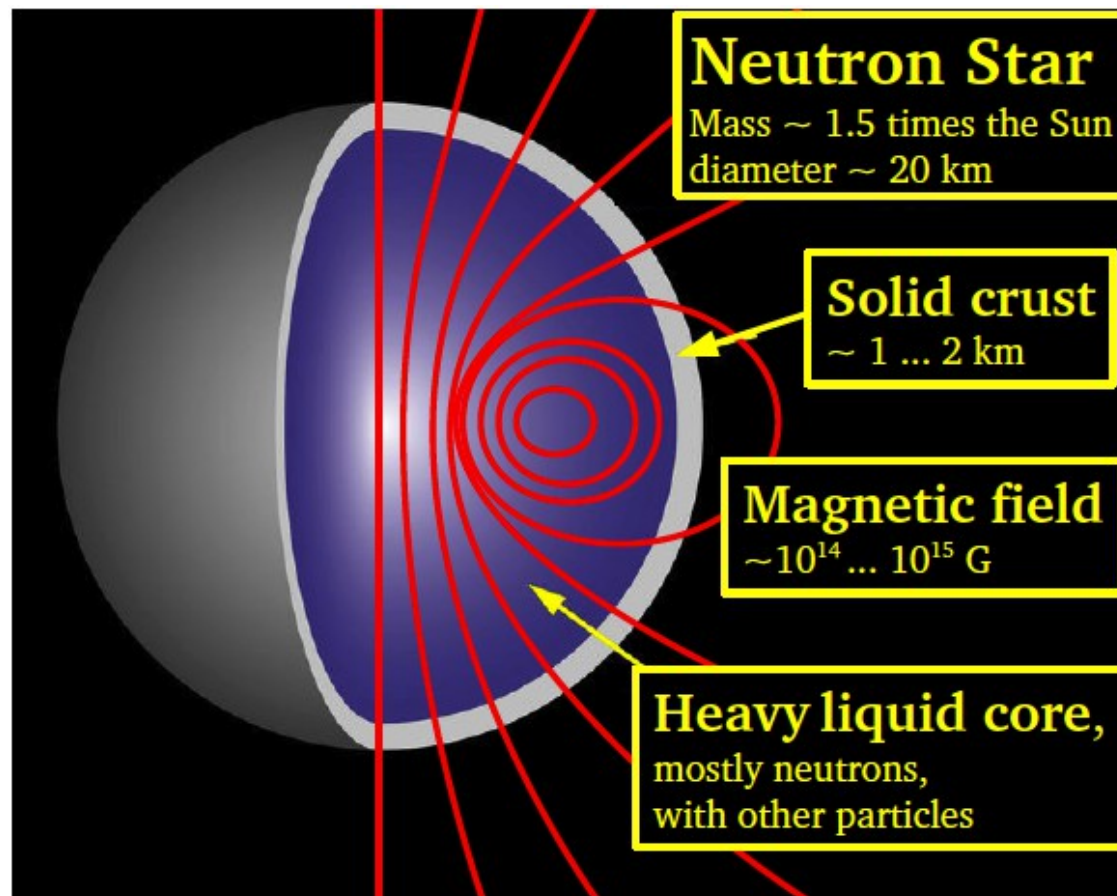
+ Explains low/high freq. QPOs
- Cannot explain all QPOs at once



Magneto-elastic model

Thin crust/no crust: Levin 2006, 2007, Sotani et al 2006, 2008, 2009, CD et al 2009, Colaiuda et al 2009, Lander & Jones 2011, Passamonti & Lander 2012

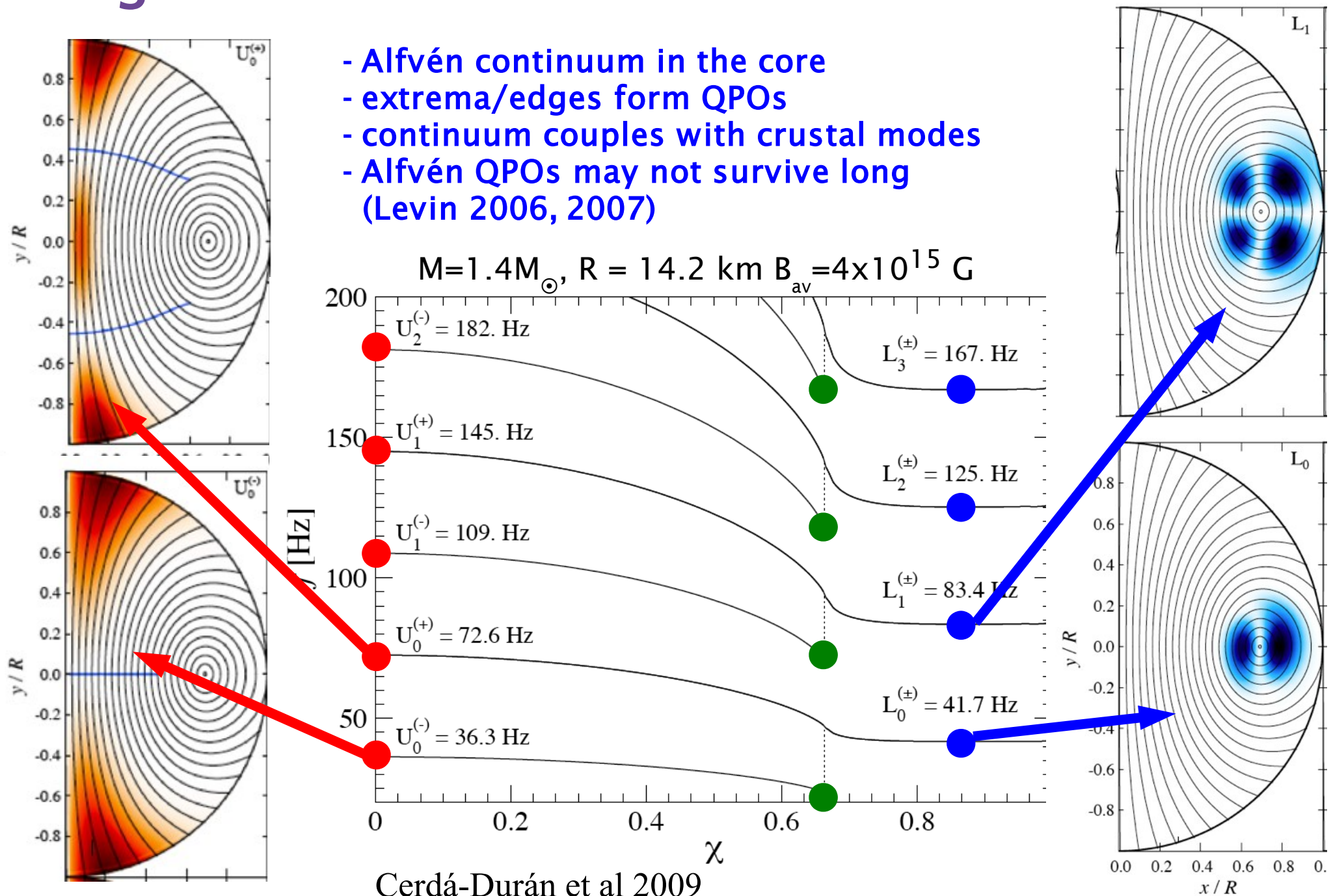
Extended crust: Glampedakis et al. 2006, Gabler et al 2011, 2012, 2013a, 2013b, Colaiuda et al 2011 & 2012, Van Hoven & Levin 2011 & 2012



Gabler et al 2012

Magneto-elastic model

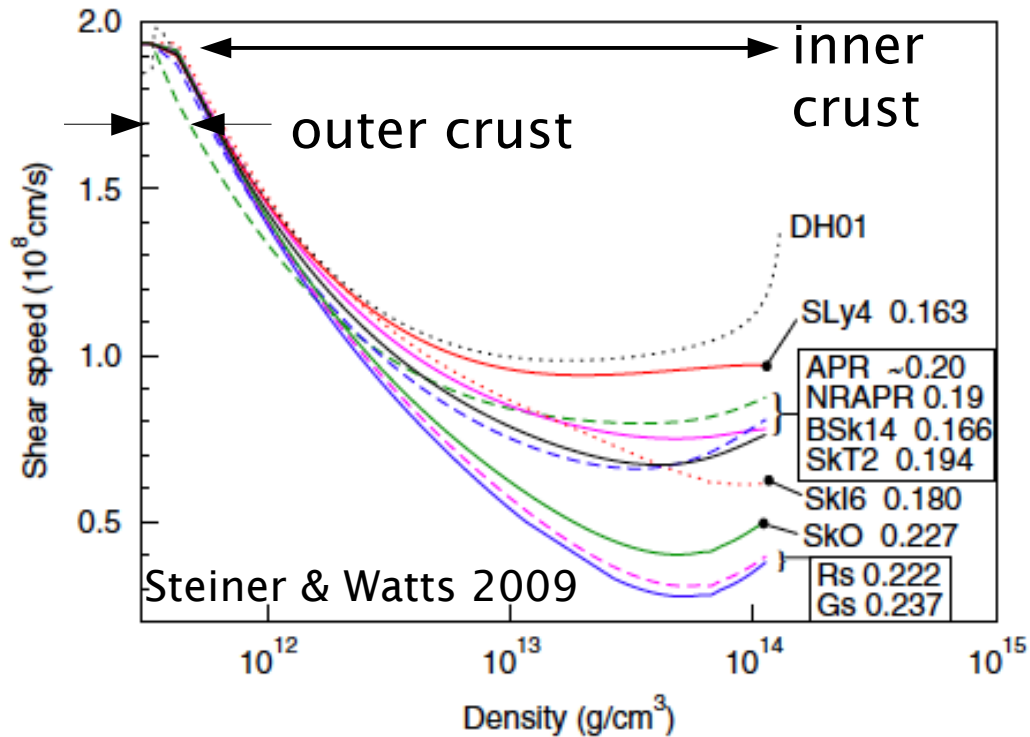
- Alfvén continuum in the core
- extrema/edges form QPOs
- continuum couples with crustal modes
- Alfvén QPOs may not survive long (Levin 2006, 2007)



Magneto-elastic model

Magneto-elastic waves (eigenvalues of the magneto-elastic equations)

$$\lambda_{me} = \pm \sqrt{\frac{B^2 + \mu_s}{\rho}}$$



$$v_{\text{Alfven}} \approx 10^8 \left(\frac{B}{10^{15} \text{ G}} \right) \left(\frac{10^{14} \text{ g cm}^{-3}}{\rho} \right)^{-1/2} \text{ cm s}^{-1}$$

$$\approx 10^9 \left(\frac{B}{10^{15} \text{ G}} \right) \left(\frac{10^{12} \text{ g cm}^{-3}}{\rho} \right)^{-1/2} \text{ cm s}^{-1}$$

$$B^2 \gg \mu_s \rightarrow \lambda_{me} \simeq \pm \frac{B}{\sqrt{\rho}} \quad \text{Alfvén wave}$$

$$B^2 \ll \mu_s \rightarrow \lambda_{me} \simeq \pm \sqrt{\frac{\mu_s}{\rho}} \quad \text{Shear wave}$$

$$B^2 \sim \mu_s \rightarrow \lambda_{me} \quad \text{Magneto-elastic wave} \rightarrow \text{Magnetars!!!}$$

Magneto-elastic simulations in general relativity

CoCoA code (CoCoNuT framework)

- 2D-axisymmetric GRMHD code
- Spherical coordinates
- Finite-volume Riemann solvers + CT methods
- Dynamical space-time (CFC)



Approximations

- Torsional oscillations
 - Low amplitude (linear)
 - Cowling (fixed spacetime)
 - Spherically symmetric background (non-rotating stars)
 - Ideal MHD
 - Axisymmetry
- } → constant density (anelastic)

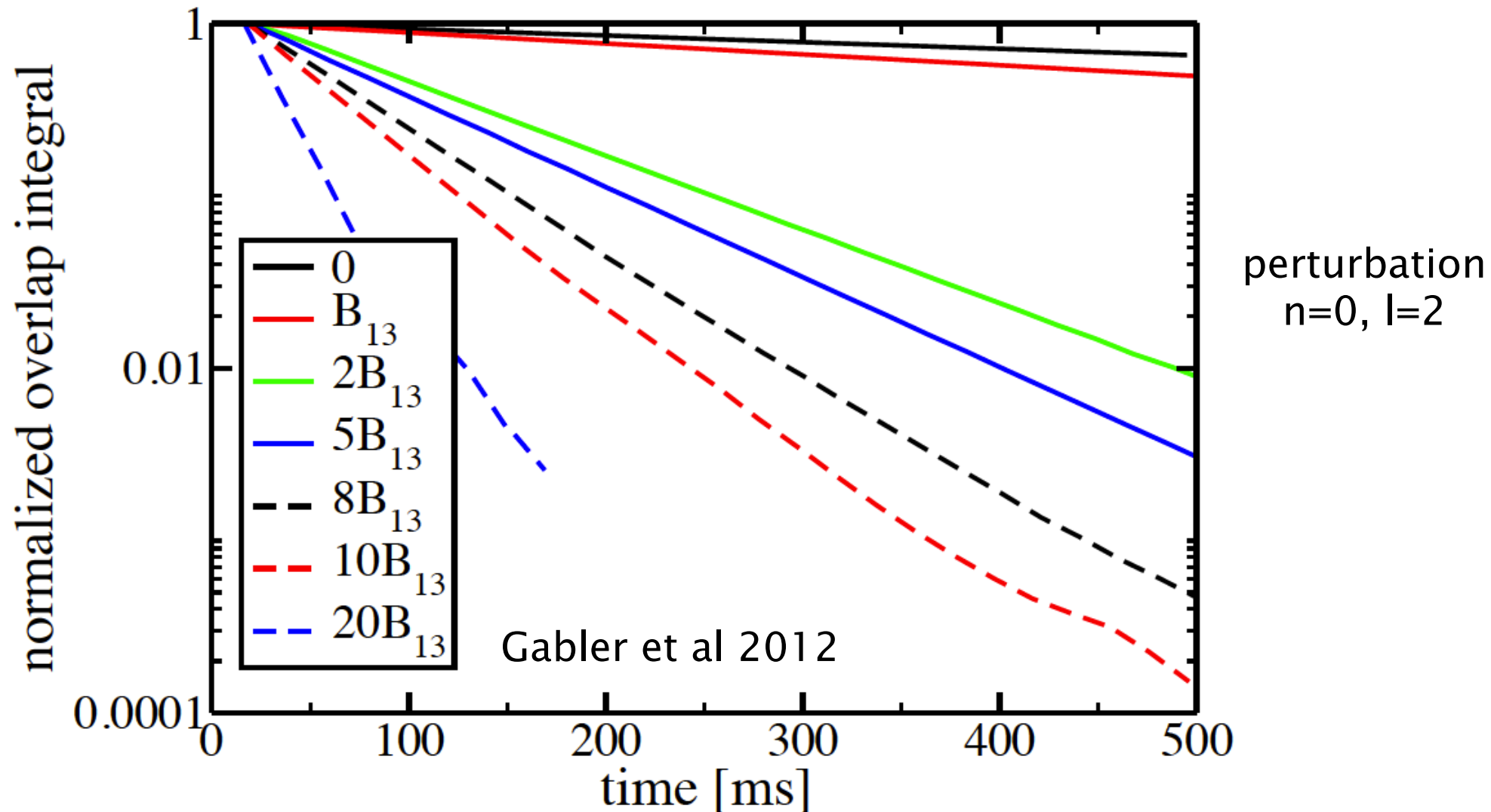
EOS

- **Core:** APR (Akmal et al 1998) and L (Pandharipande & Smith 1975)
- **Crust:** NV (Negele & Vautherin 1973) and DH (Douchin & Hansel 2001)

Absorption of crustal shear modes by the Alfvén continuum

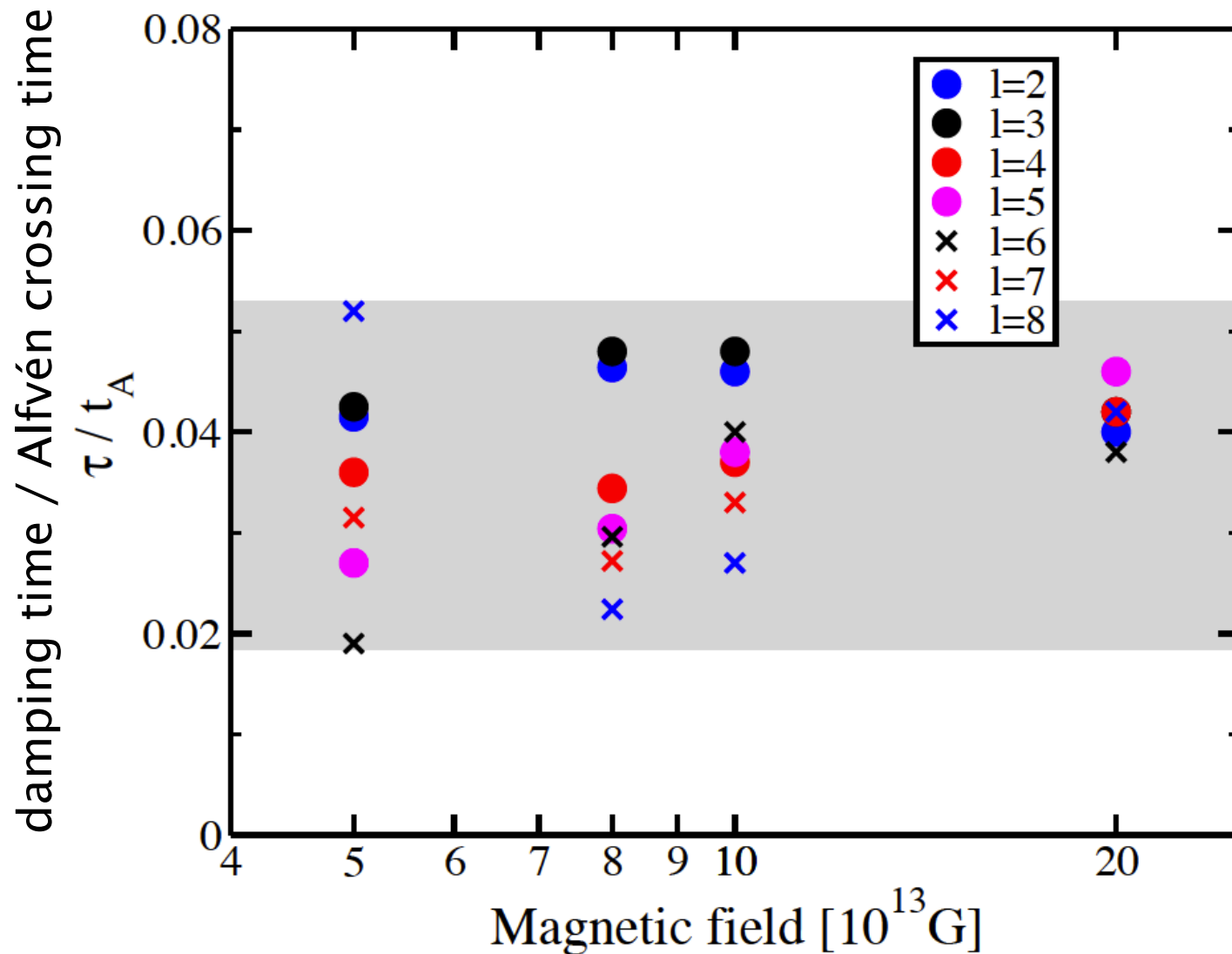
EoS: APR+DH, shear modulus: DH, $M=1.4M_{\odot}$, $R=12.1$ km, $\Delta R=0.88$ km

Dipolar-like magnetic field, no toroidal component



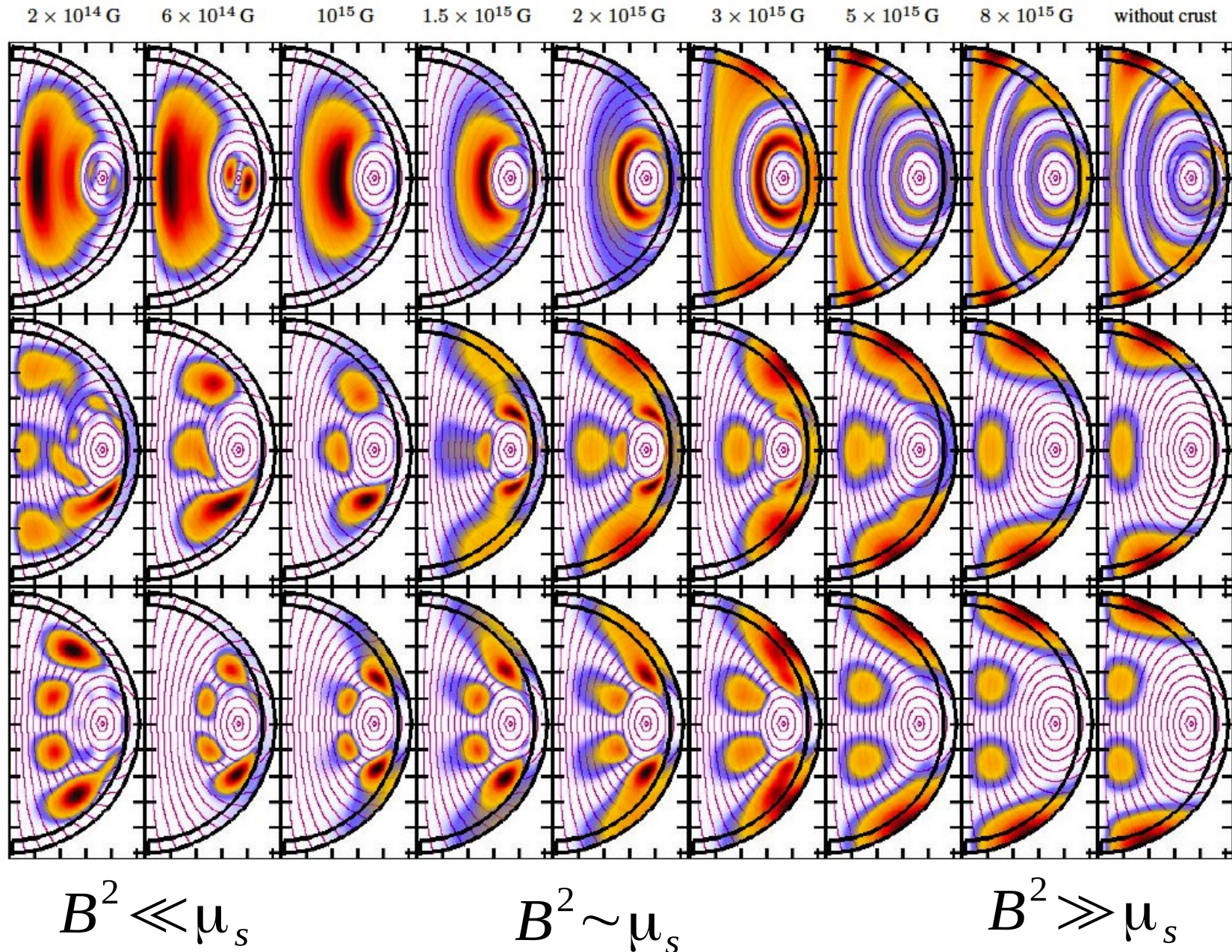
Similar for other EoS, shear modulus and mass

Absorption of crustal shear modes by the Alfvén continuum



Gabler et al 2012

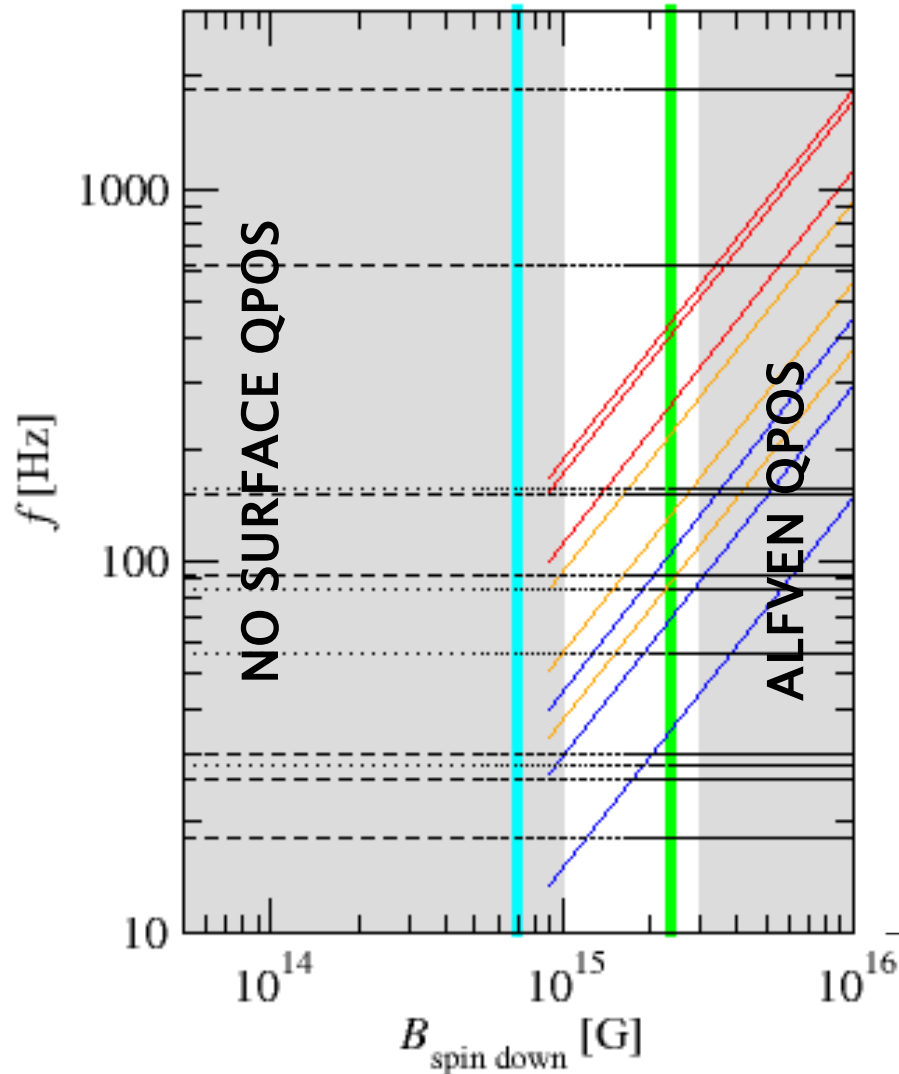
QPOs in the Alfvén continuum



Gabler et al 2012

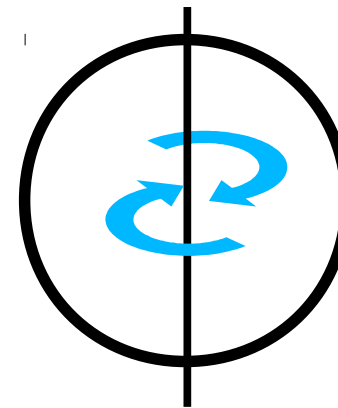
Increasing magnetic field

Axial vs polar modes

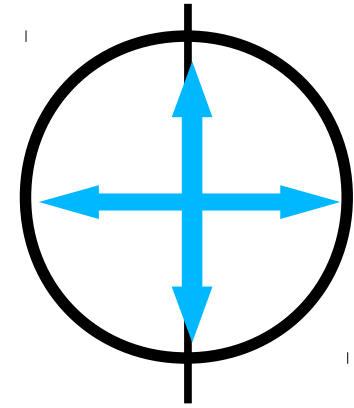


- axial, $m=0$ (Sotani et al 2008, CD et al 2009, Gabler et al 2011, Colaiuda & Kokkotas 2012, Gabler et al 2013)
- polar, $m=0$ (Sotani & Kokkotas 2009, Colaiuda & Kokkotas 2012)
- polar, $m=2$ (Lander & Jones 2011, Passamonti & Lander 2012)
- SGR1806-20 (Dec. 27, 2004)
- SGR1900+14, Aug. 27 1998

- Magneto-elastic regime is the most relevant
- polar oscillations x5 larger frequency than axial
- **Not possible to explain high and low frequency QPOs at the same time** (unless very high order QPOs are considered)



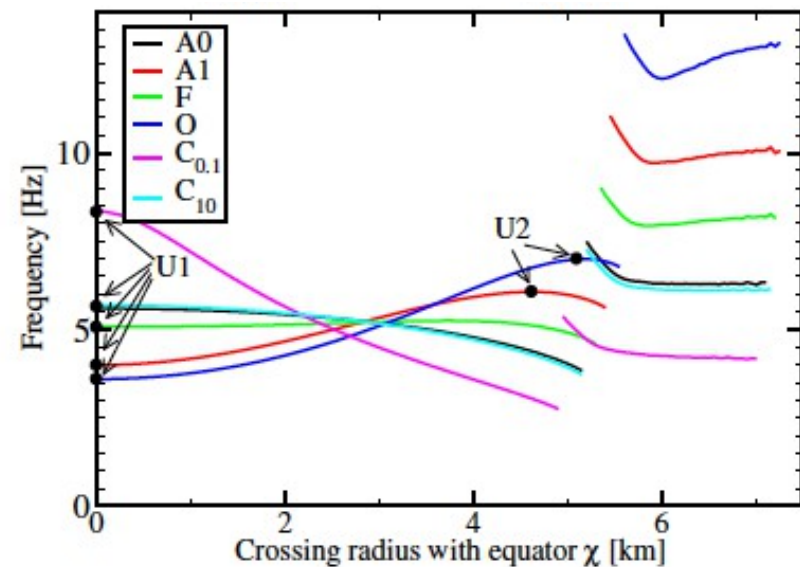
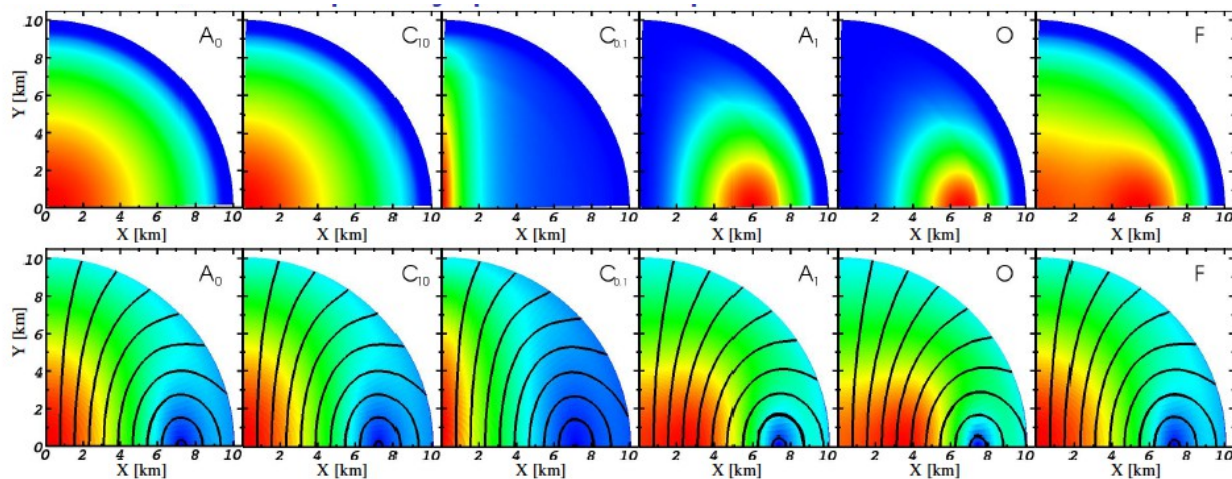
axial (torsional)



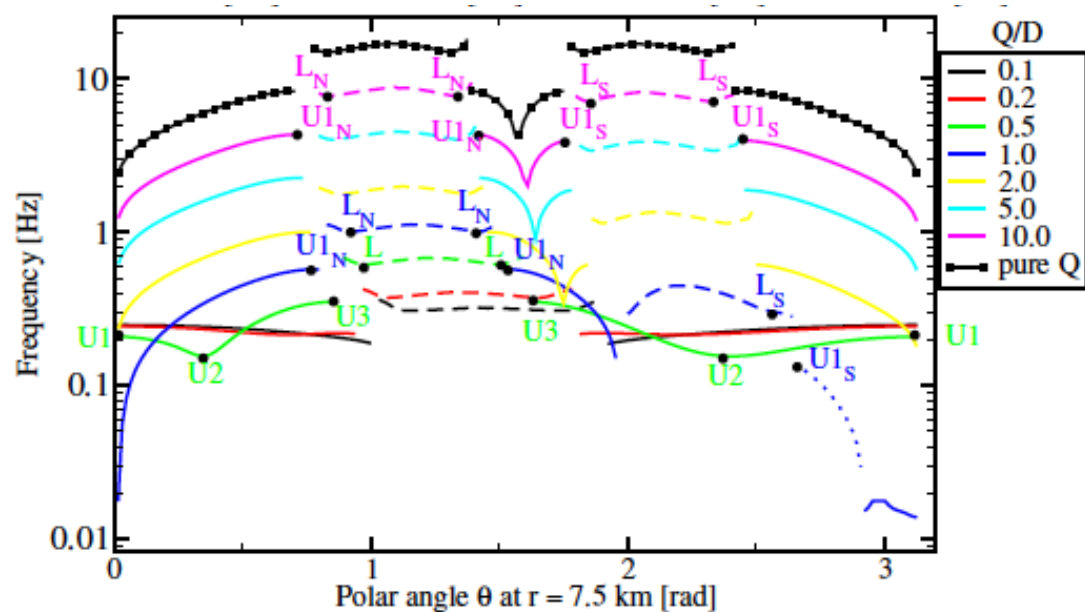
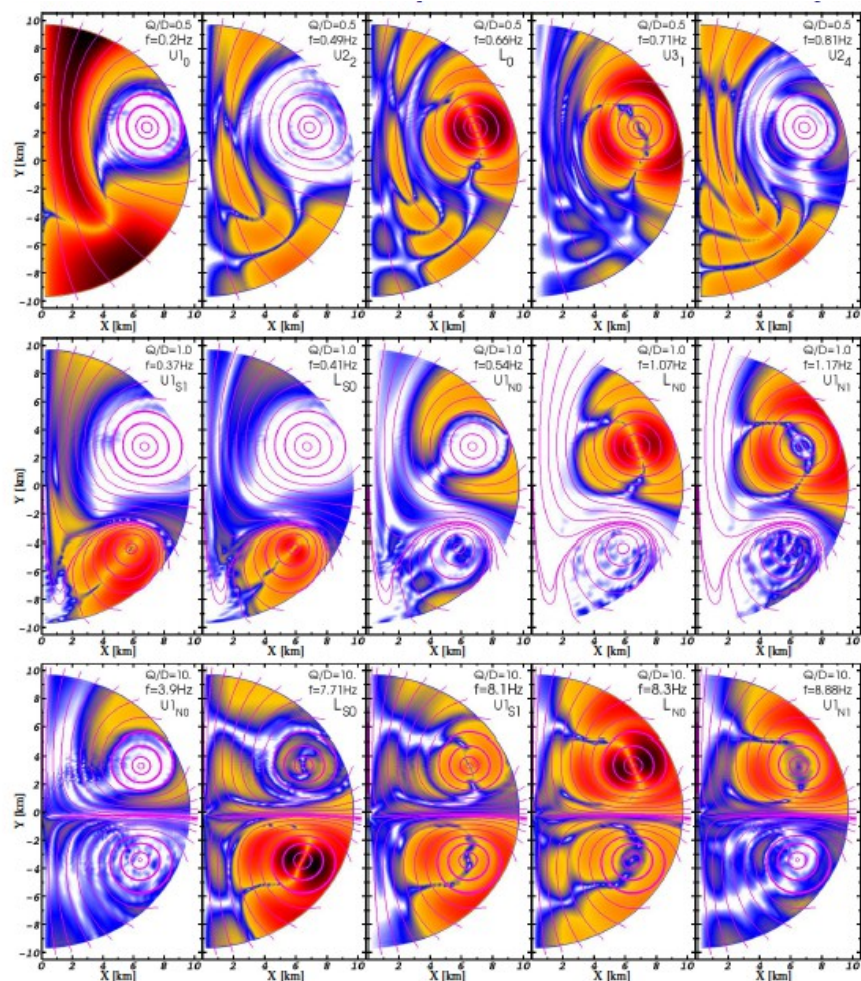
polar

— SGR1806-20

— SGR1900+14

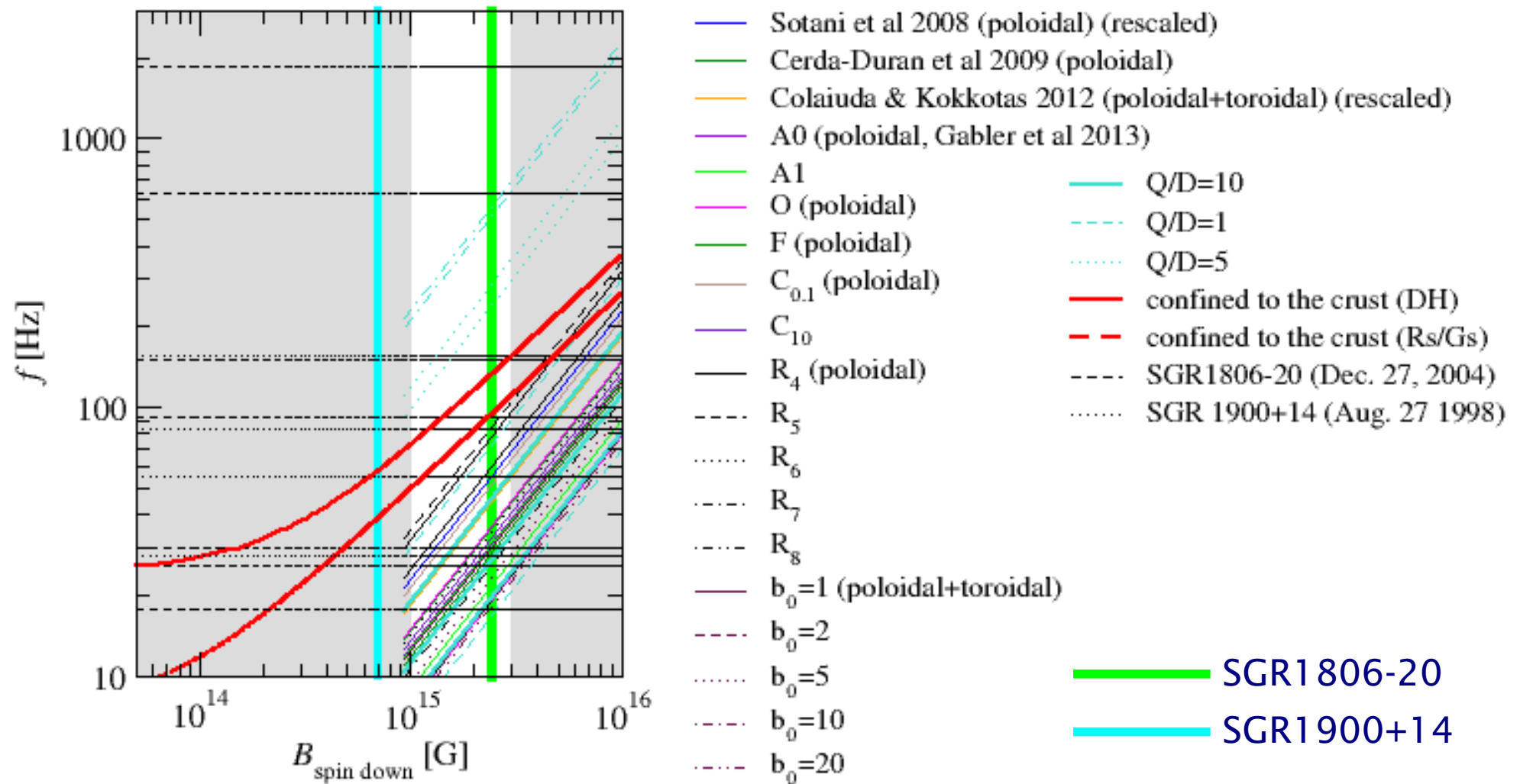


Magnetic field structure



Gabler et al 2013

Magnetic field structure



- Dipole-like configurations: x3 differences in frequency, multiple QPOs
- High order multipoles can increase the frequency
- Magnetic field confined to the crust cannot explain QPOs
- Not possible to explain high and low frequency QPOs at the same time.

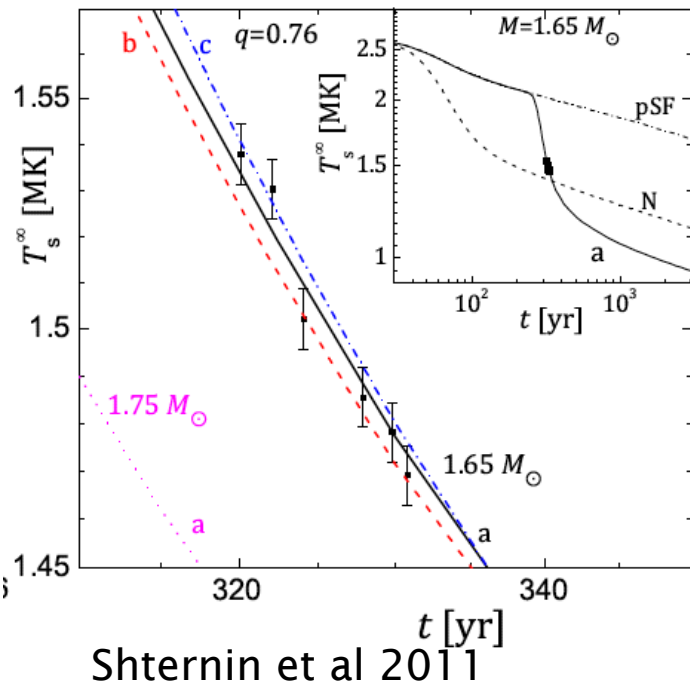
Summary (but not the end)

- **Frequency of Alfvén QPOs is a degenerate problem**
 - Magnetic field strength and structure
 - Equation of state
 - Mass
- **Alfvén QPO model of non-superfluid cores has problems**
 - Not possible to accommodate high and low frequency QPOs at the same time.
 - Are Alfvén QPOs long lived? (Levin 2006, 2007)

Superfluidity

Gabler et al 2013 (arxiv:1304.2566)

Superfluidity



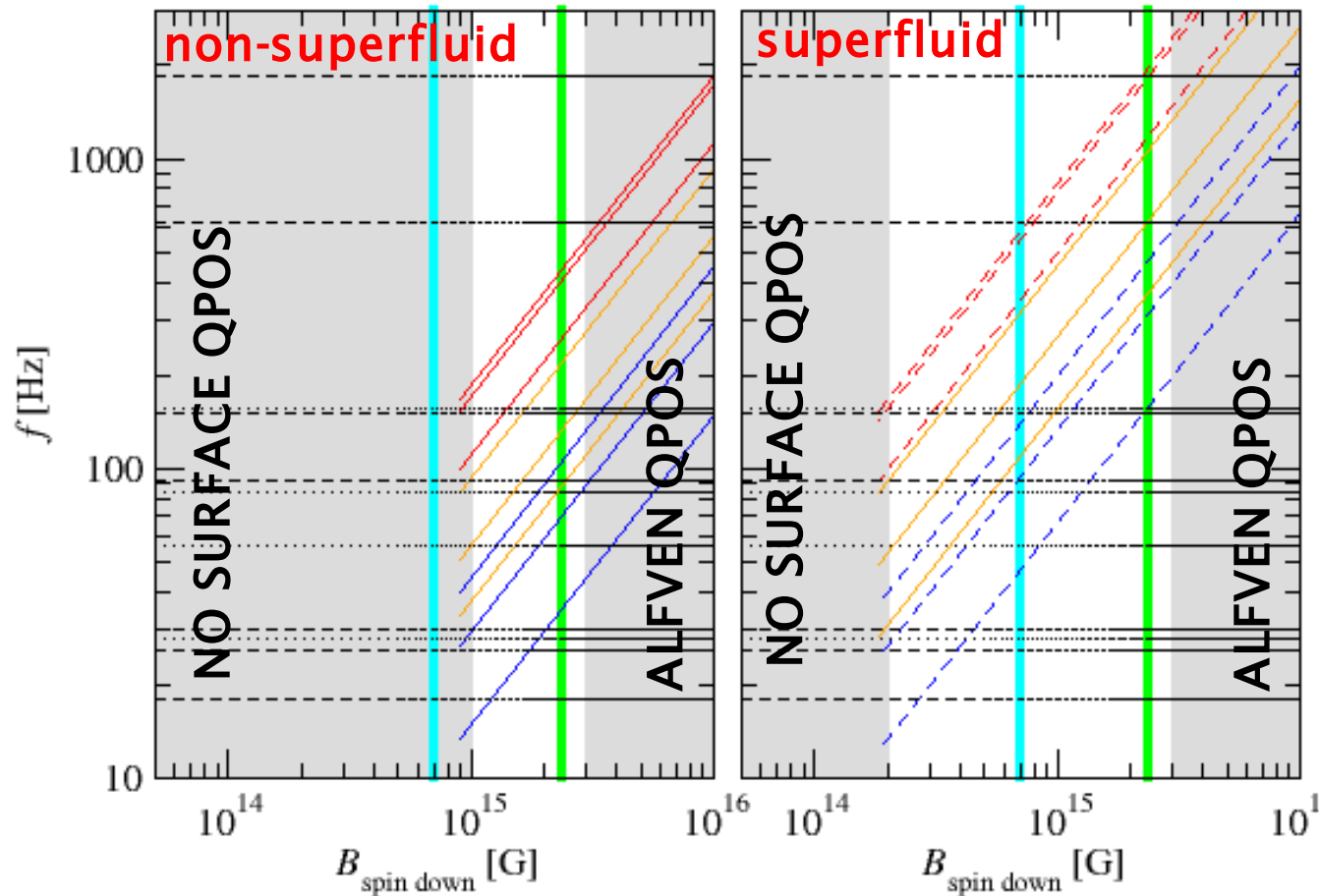
- Superfluidity is favored in NS (Baym et al 1969).
- Explanation for pulsar glitches (Anderson & Itoh 1975). However anti-glitch (Archibald 2013).
- Cooling curve of Cas A consistent with superfluid core (Shternin et al 2011, Page et al 2011).
- Superconductivity may be suppressed in magnetars since $B_{\text{crit}} \sim 10^{15} - 10^{16}$ G (Glampedakis et al 2011).
- Only protons are involved in Alfvén waves
- Glampedakis et al 2006, van Hoven et al 2011, 2012, Gabler et al 2013

$$v_{\text{Alfvén}, SP} = \pm \frac{B}{\sqrt{X_p \rho}} \sim 5 \left(\frac{X_p}{0.05} \right)^{-1/2} v_{\text{Alfvén}, normal}$$

Alfvén QPO frequency increases a factor 5

→ can explain QPO frequencies with 1/5 magnetic field strength

Superfluid vs non-superfluid (simplified)



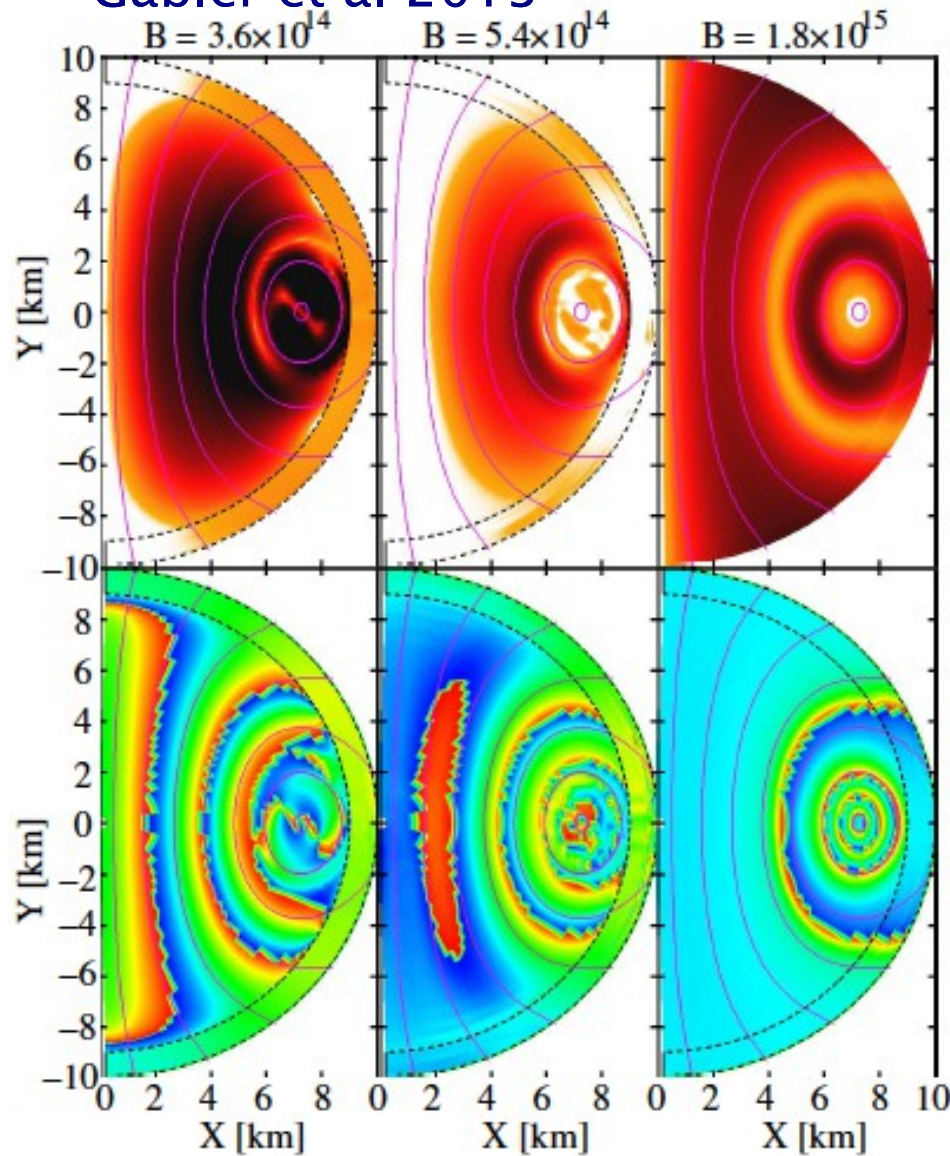
- increase frequency x5
- broader magneto-elastic region

- axial, $m=0$ (Sotani et al 2008, CD et al 2009, Gabler et al 2011, Colaiuda & Kokkotas 2012)
- polar, $m=0$ (Sotani & Kokkotas 2009, Colaiuda & Kokkotas 2012)
- polar, $m=2$ (Lander & Jones 2011, Passamonti & Lander 2012)
- SGR1806-20 (Dec. 27, 2004)
- SGR1900+14, Aug. 27 1998

- SGR1806-20
- SGR1900+14

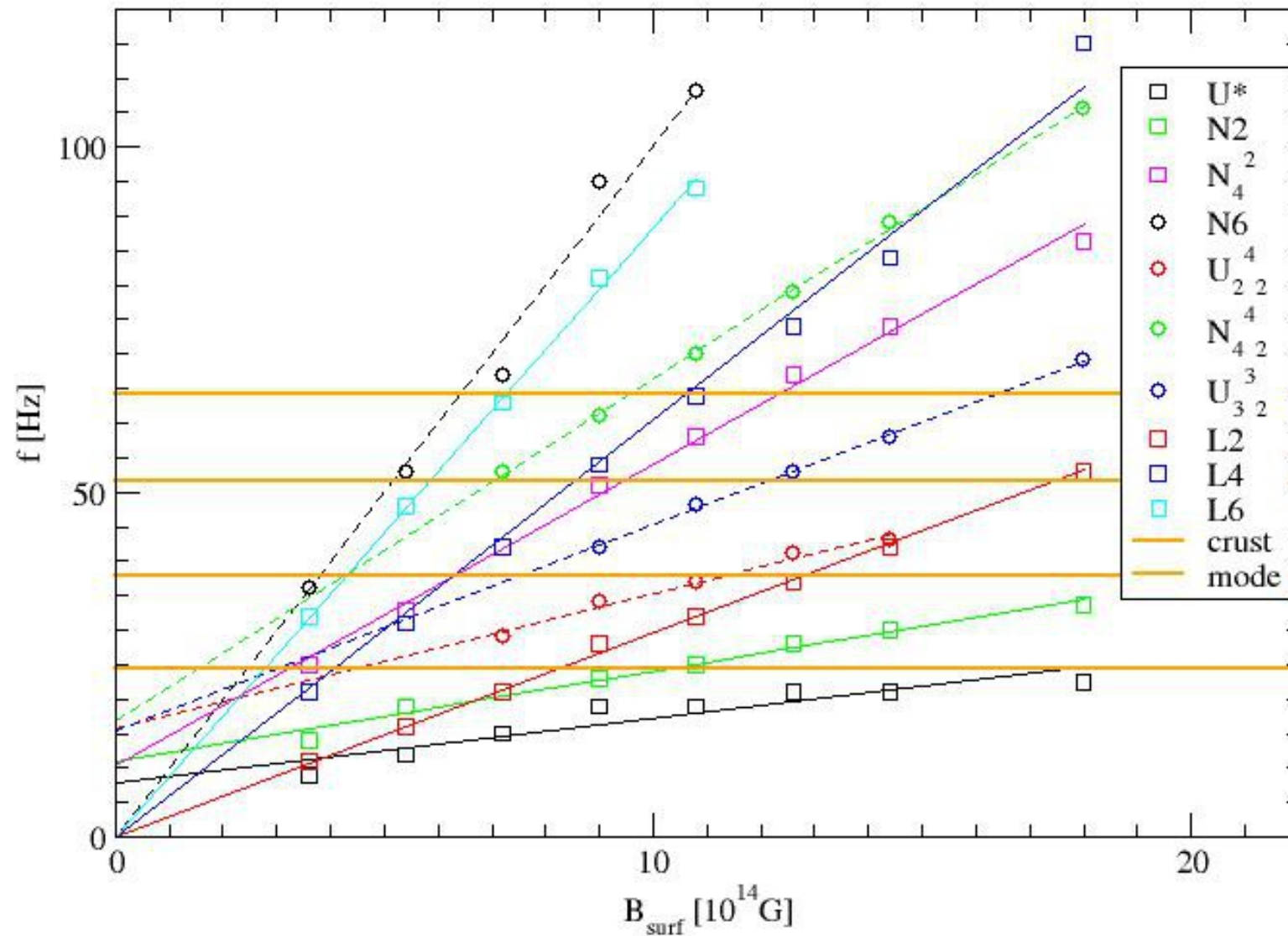
Magneto-elastic simulations of superfluid cores

Gabler et al 2013

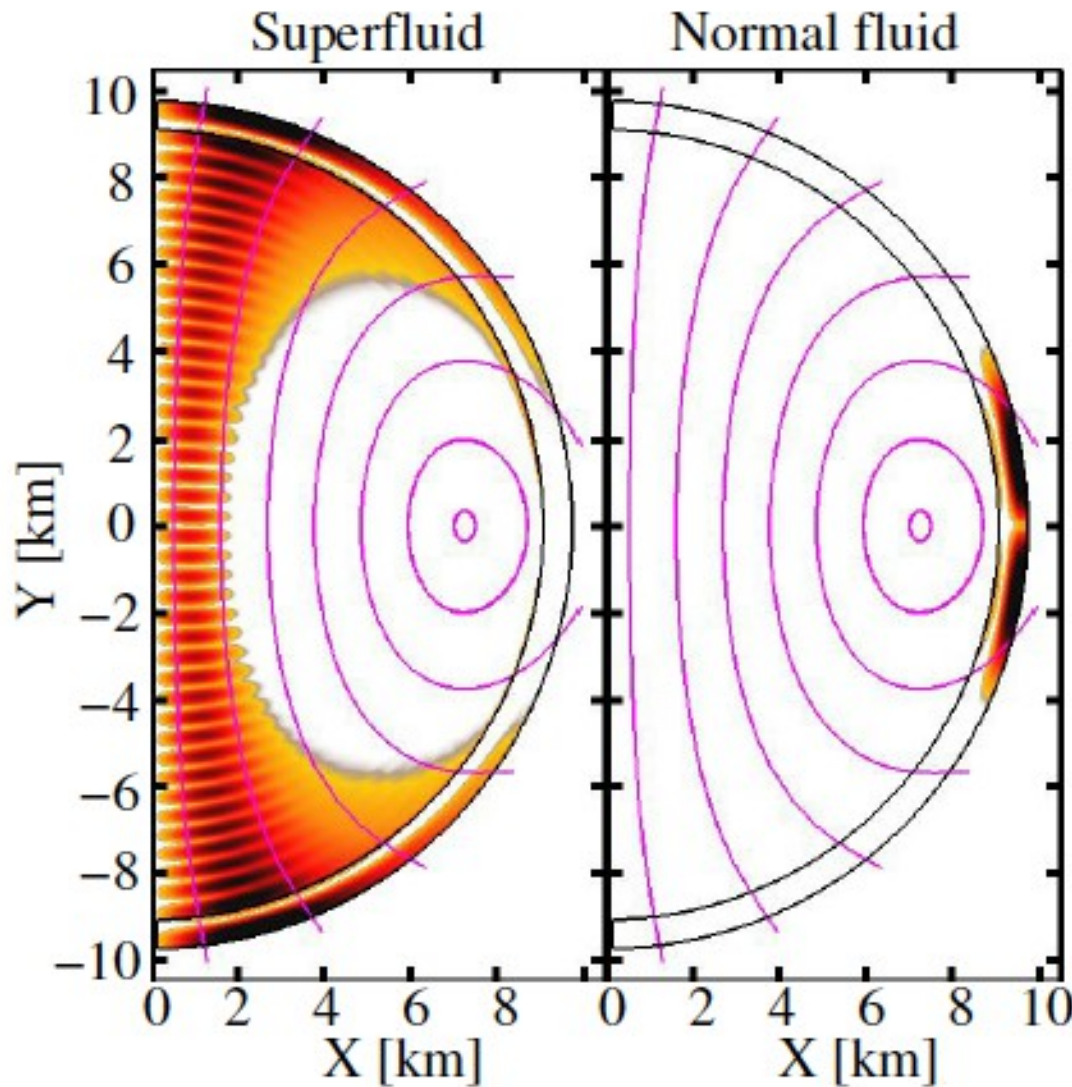


- Constant-phase global QPOs (modes?)
- long lived: >200 Alfvén crossing times
- Resonance between crustal shear modes and the Alfvén continuum
- Appear generically for broad range of B ($5 \times 10^{14} - 5 \times 10^{15}$ G)
- Is possible to get similar features in non-superfluid models fine-tuning B.
- van Hoven et al 2010, 2012 $\rightarrow$ crustal modes in gaps of Alfvén continua? $\rightarrow$ different interpretation?

Magneto-elastic simulations of superfluid cores



Magneto-elastic simulations of superfluid cores



Gabler et al 2013

- Long lived (>1000 cycles) resonances appear for $n=1$ modes (high frequency)
- Fine-tuned resonances in non-superfluid cores is possible but structure cannot explain observations.

Conclusions

- **A superfluid component in the core can explain QPOs in SGRs**
 - Low (<150 Hz) and high (>500 Hz) QPOs at the same time.
 - Only fundamental ($n=0,2$) and a few overtones needed.
 - Long-lived constant-phase modes.
 - Broad range of magnetic fields compatible with observations.
- **It is difficult to explain observations with a non-superfluid core.**
 - Not possible to accommodate high and low frequency QPOs at the same time.
 - Are Alfvén QPOs long lived? (Levin 2006, 2007)
 - Fine tuning required to get resonances (non-generic)
- **We need more/better observations:**
 - QPOs in normal flares?
 - new giant flares?

