



UNIVERSITY OF  
CAMBRIDGE



# Probing Black Holes with X-ray Reverberation – New observational tools?

Dan Wilkins

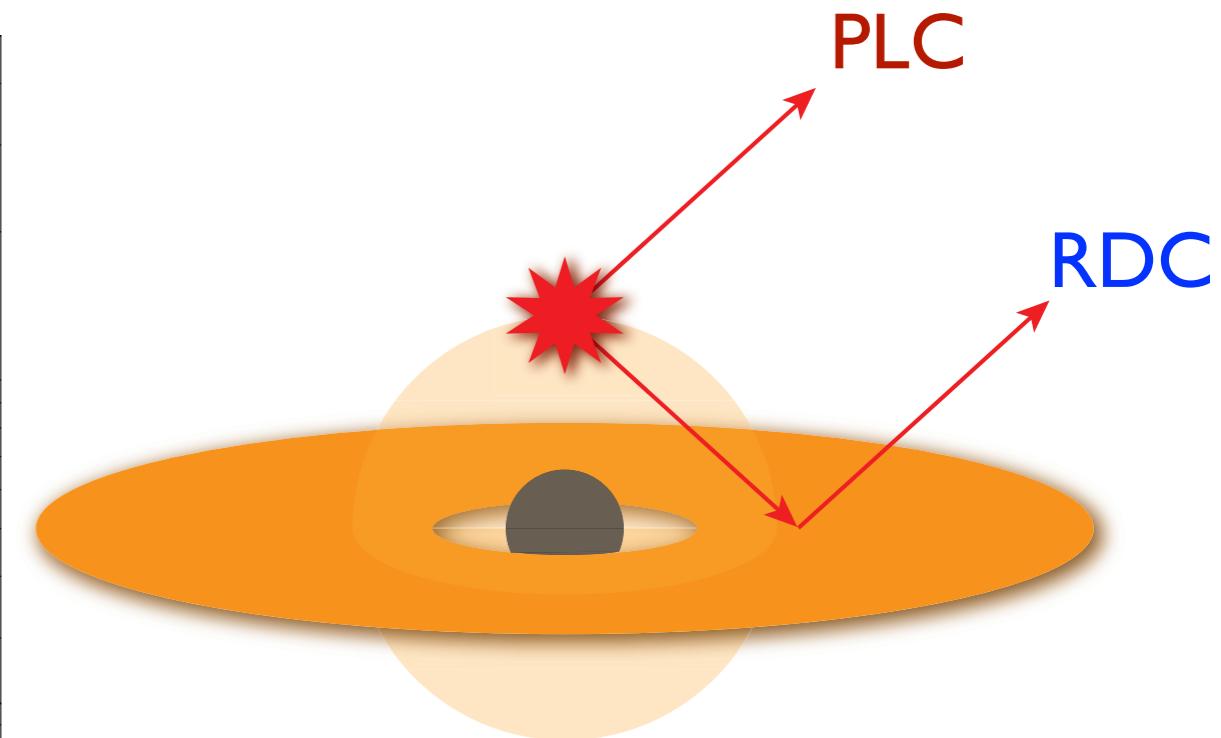
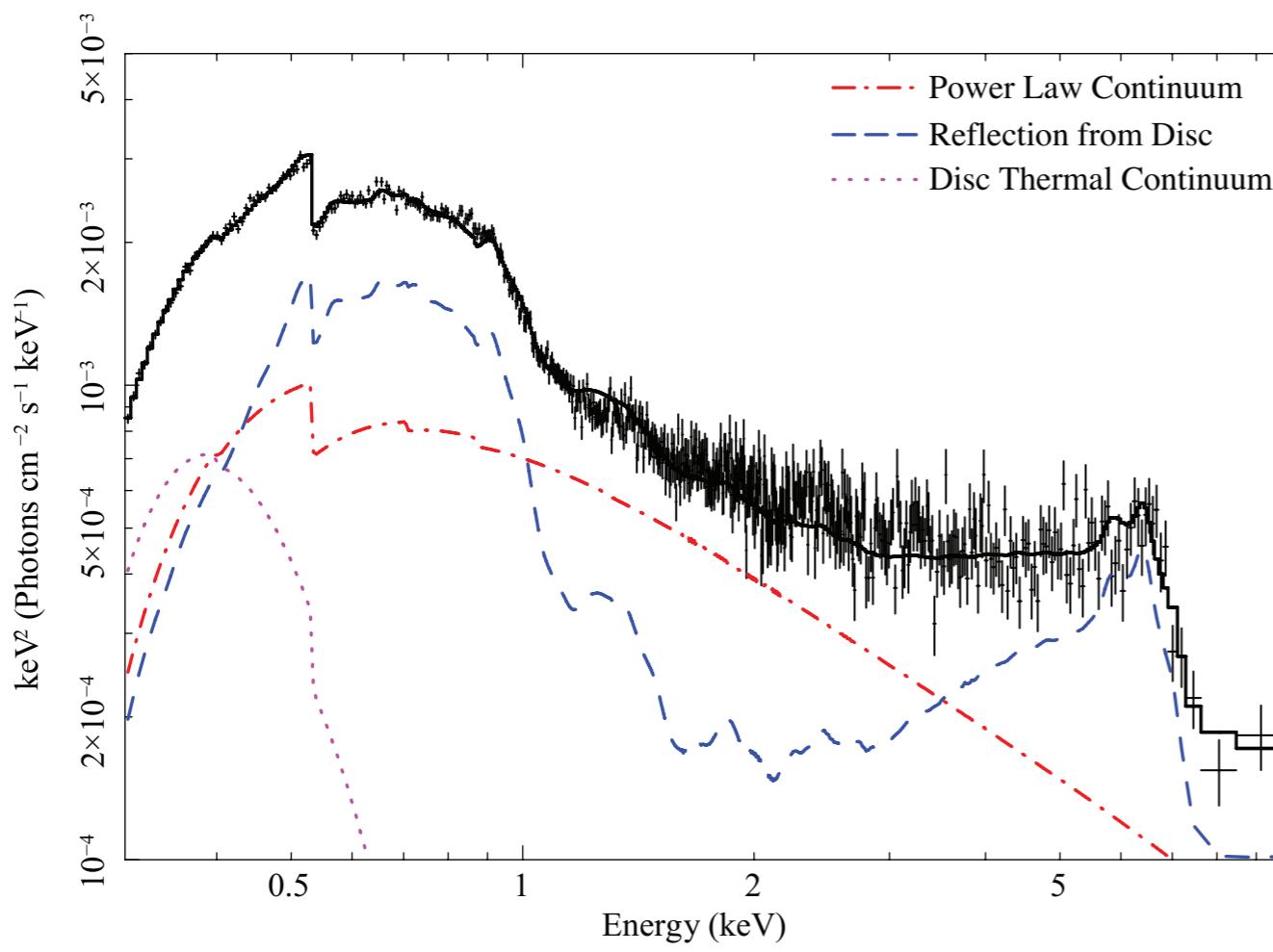
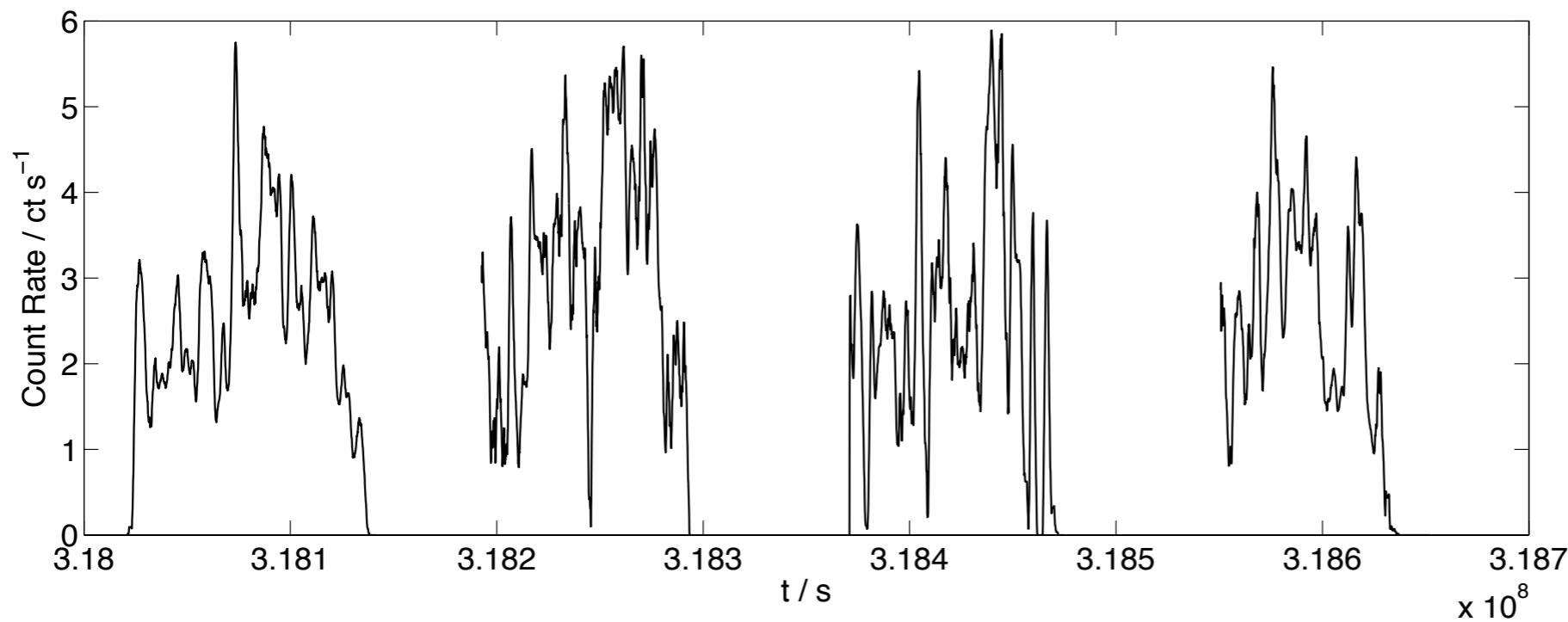
with Andy Fabian, Erin Kara, Phil Uttley, Ed Cackett

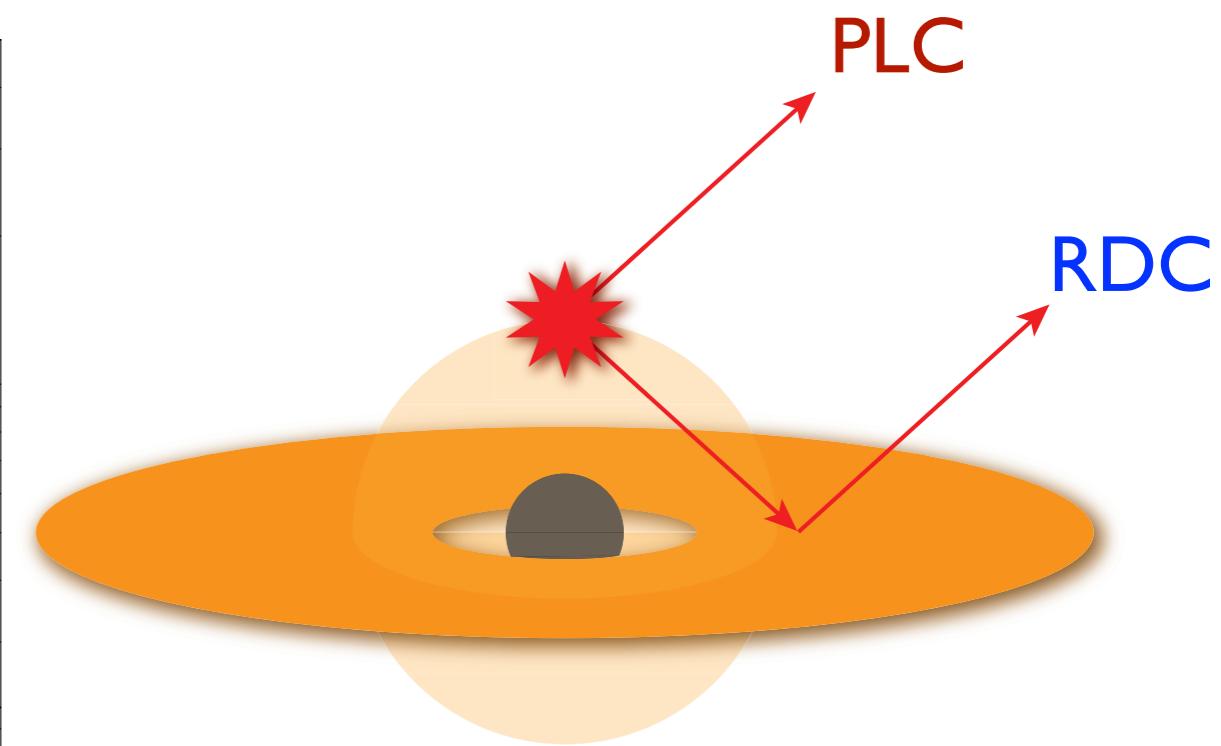
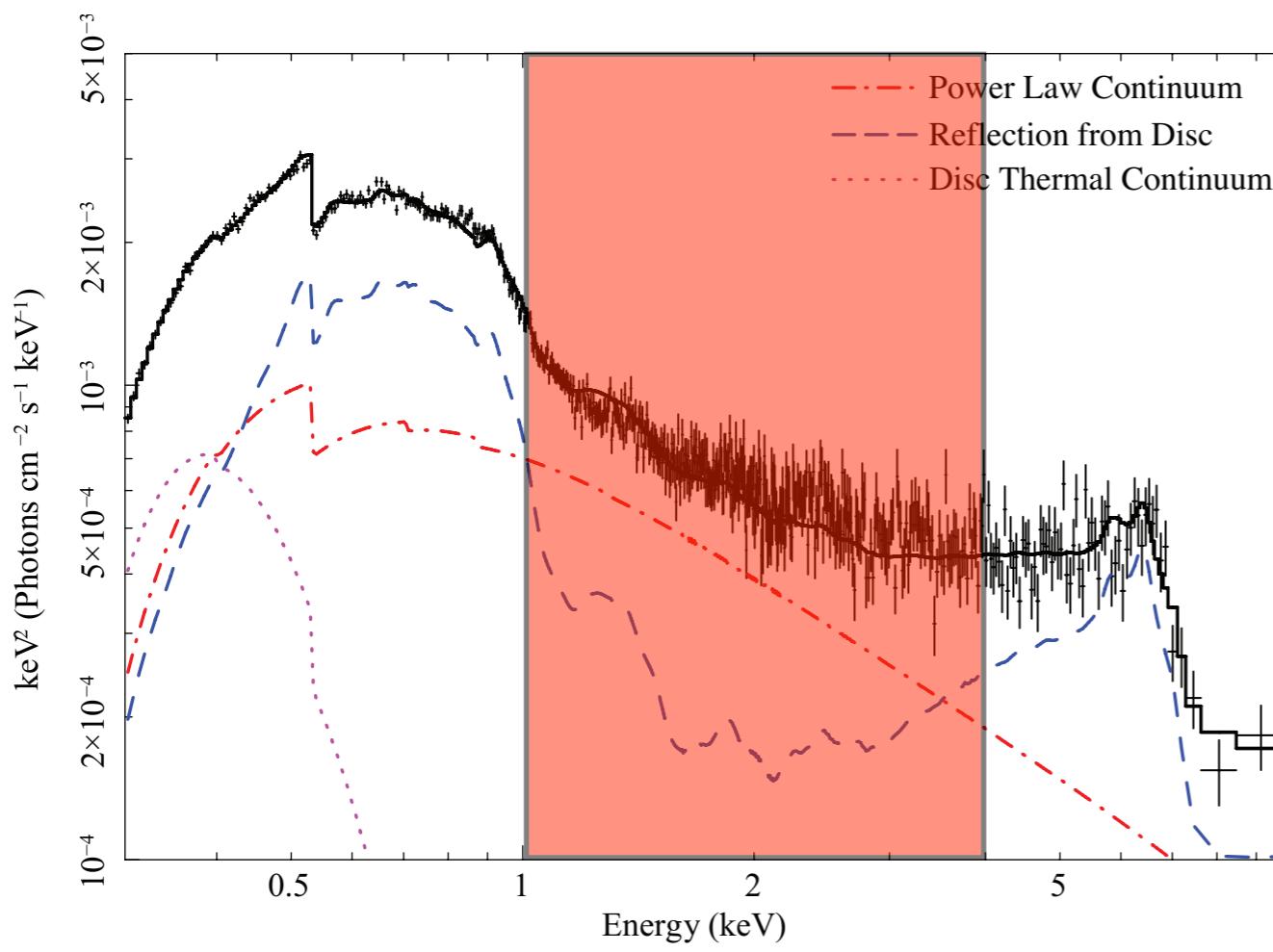
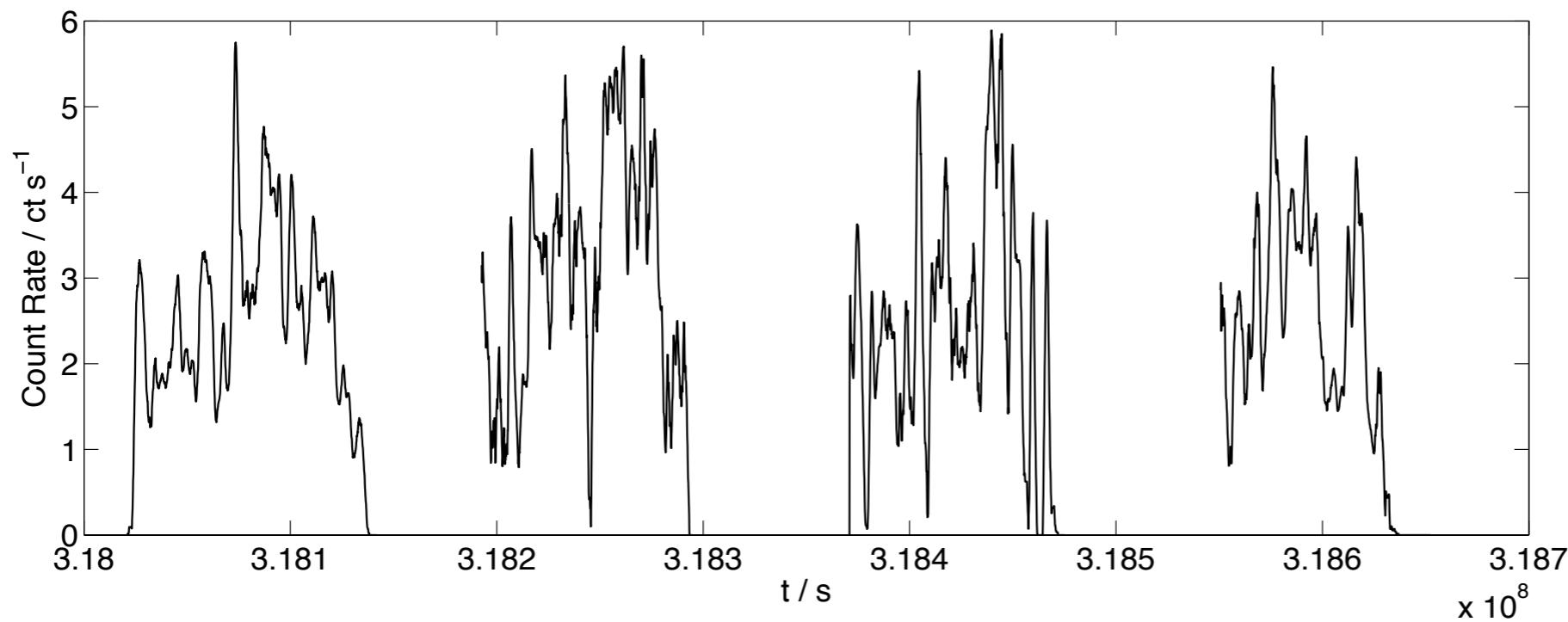
LOFT UK Science Meeting – RAS, June 2013

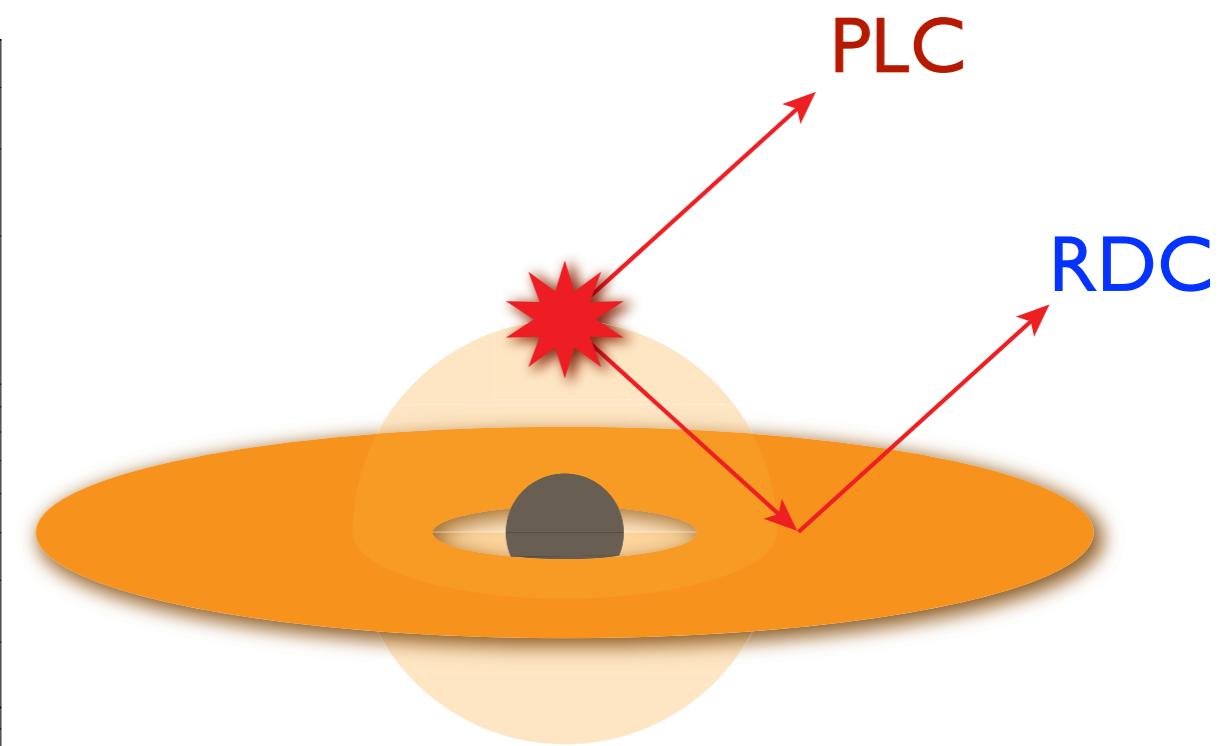
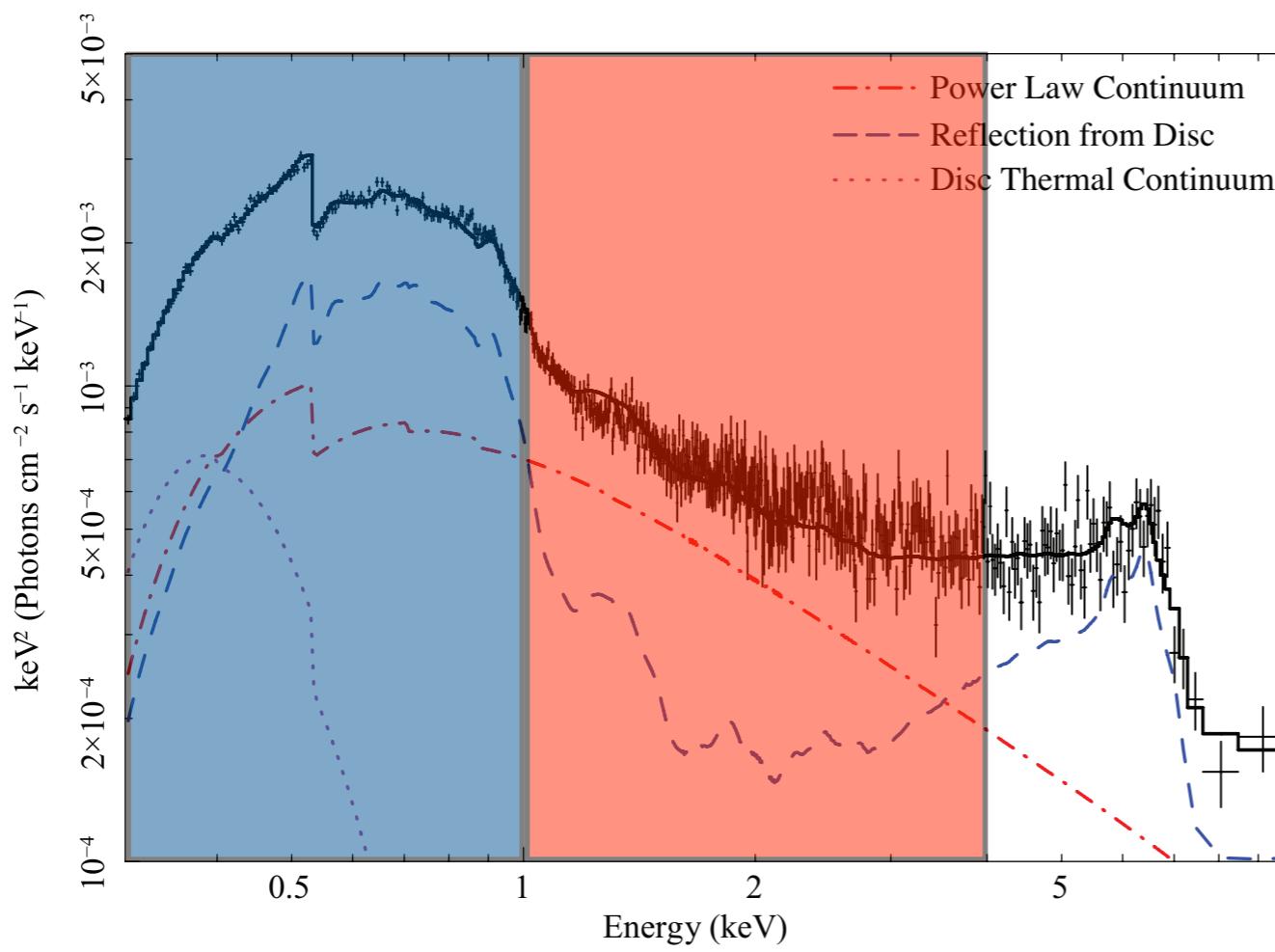
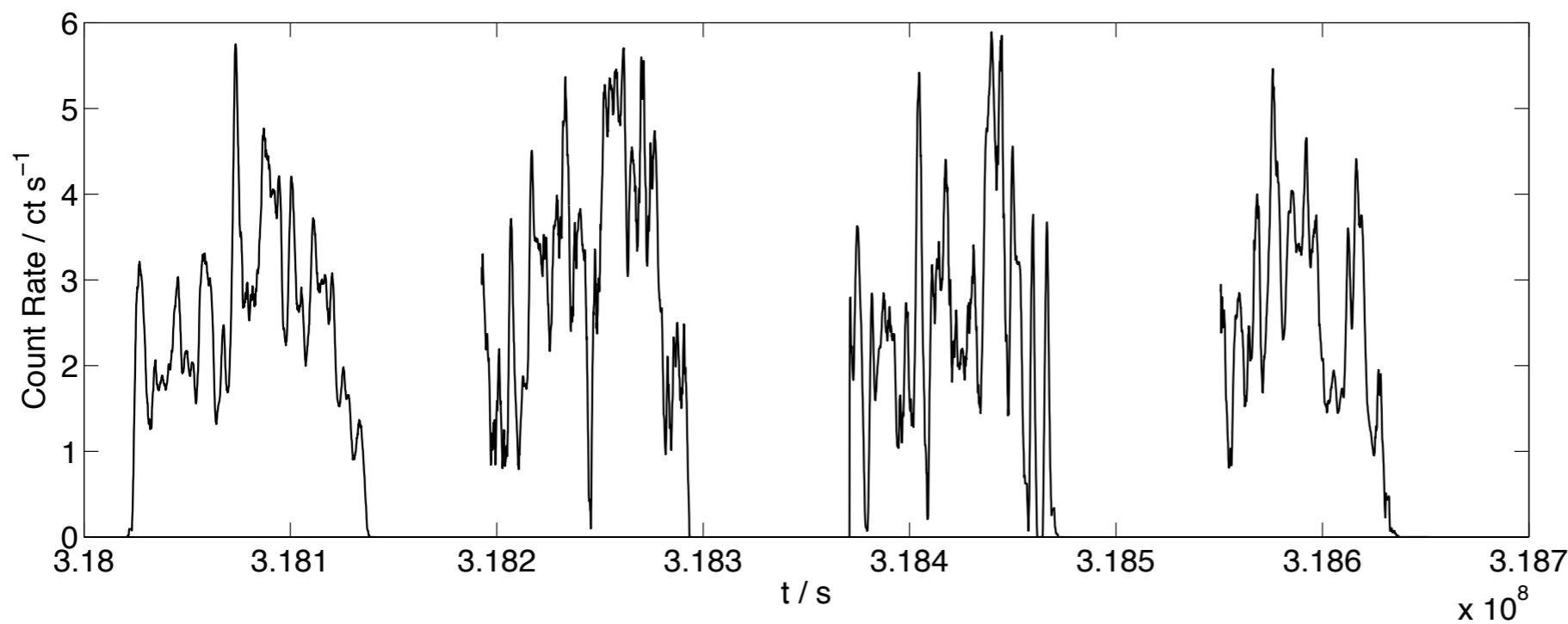


# Outline

1. Current results from (separate) energy and timing analysis
2. Energy dependence of lags
3. Predicting lag/energy spectra
4. Simultaneous lag/energy fitting as an observational tool

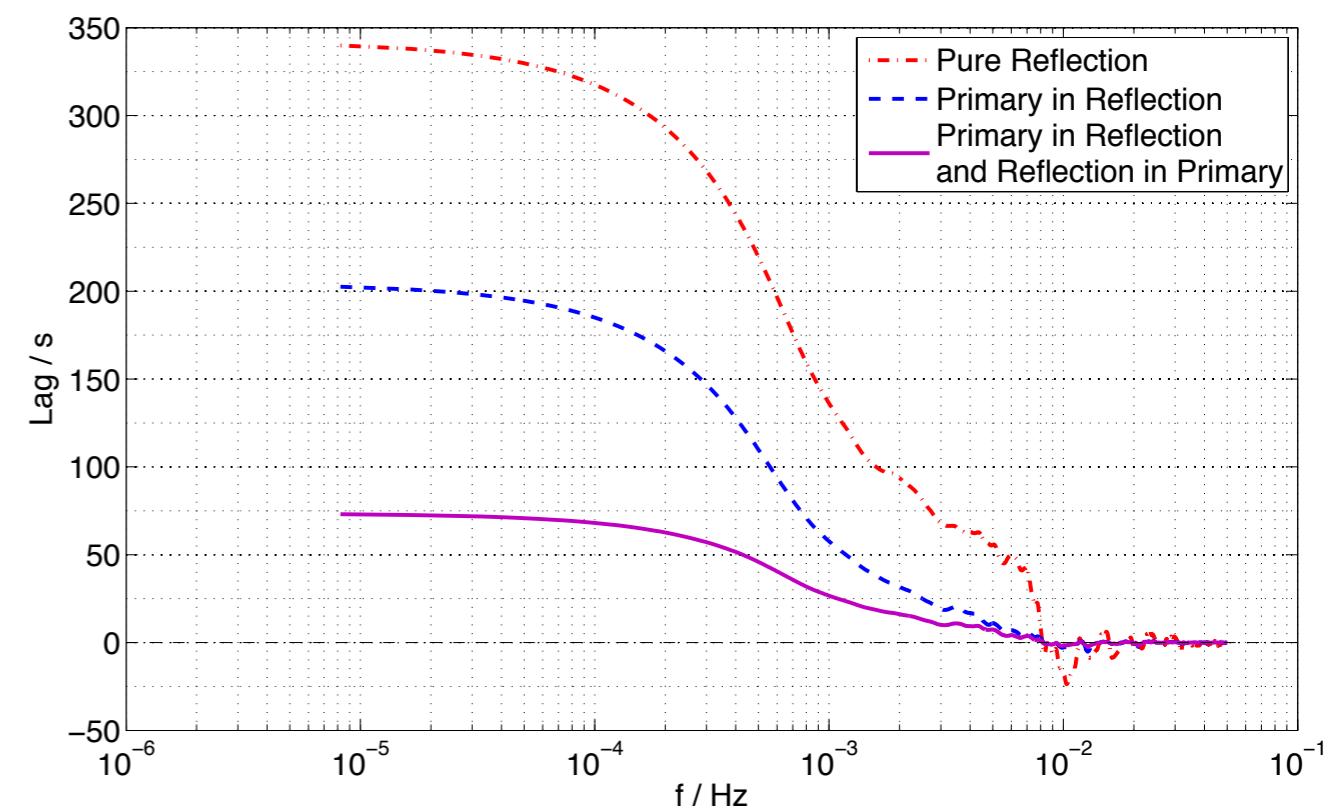
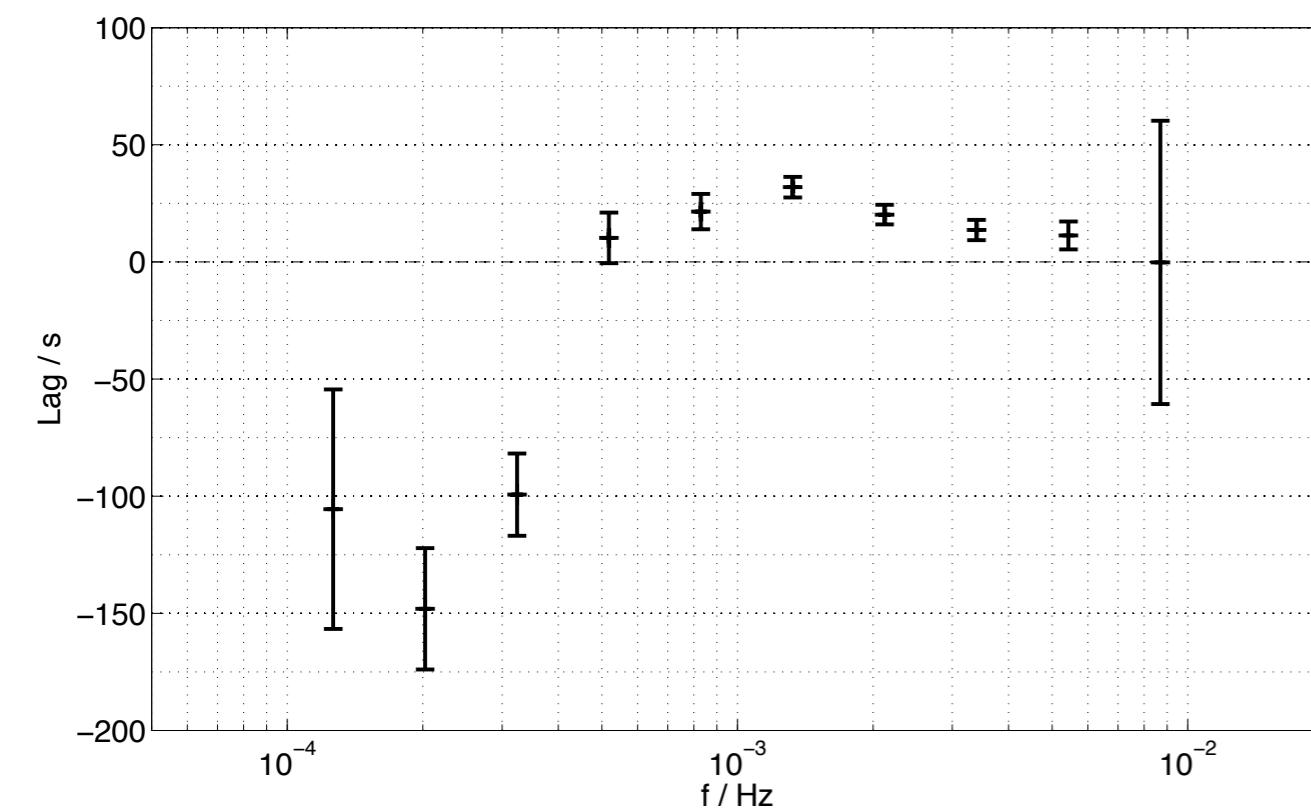






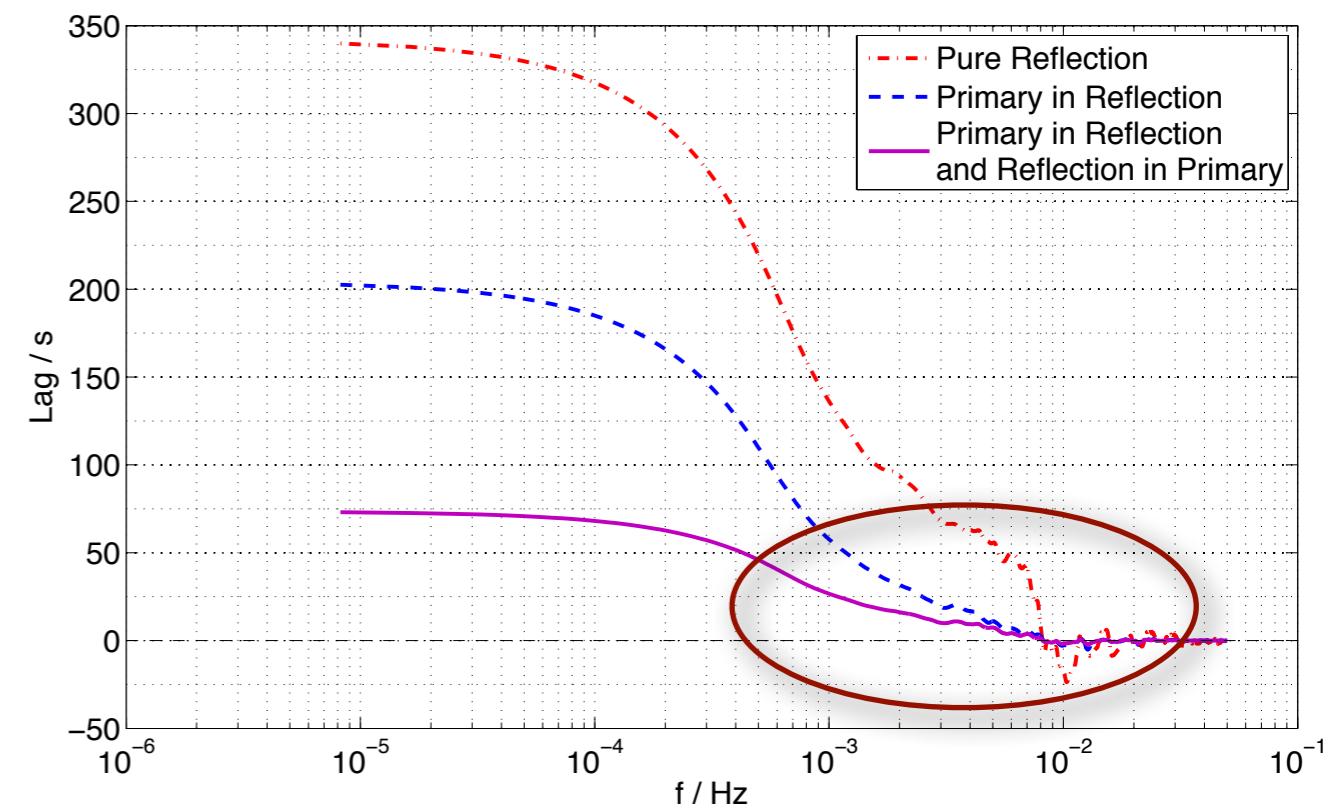
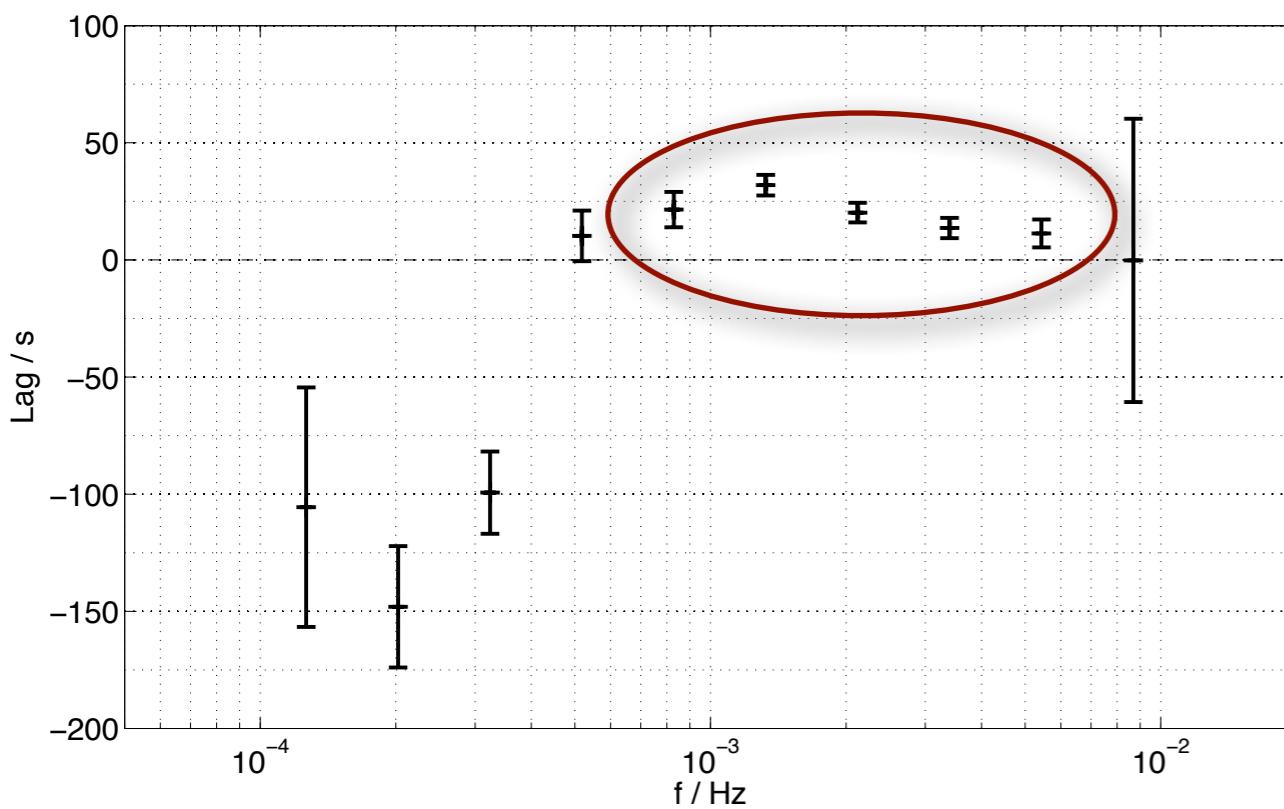
# We found reverberation lags...

Fabian+2009, Zoghbi+2010, Kara+2012, Wilkins & Fabian 2013



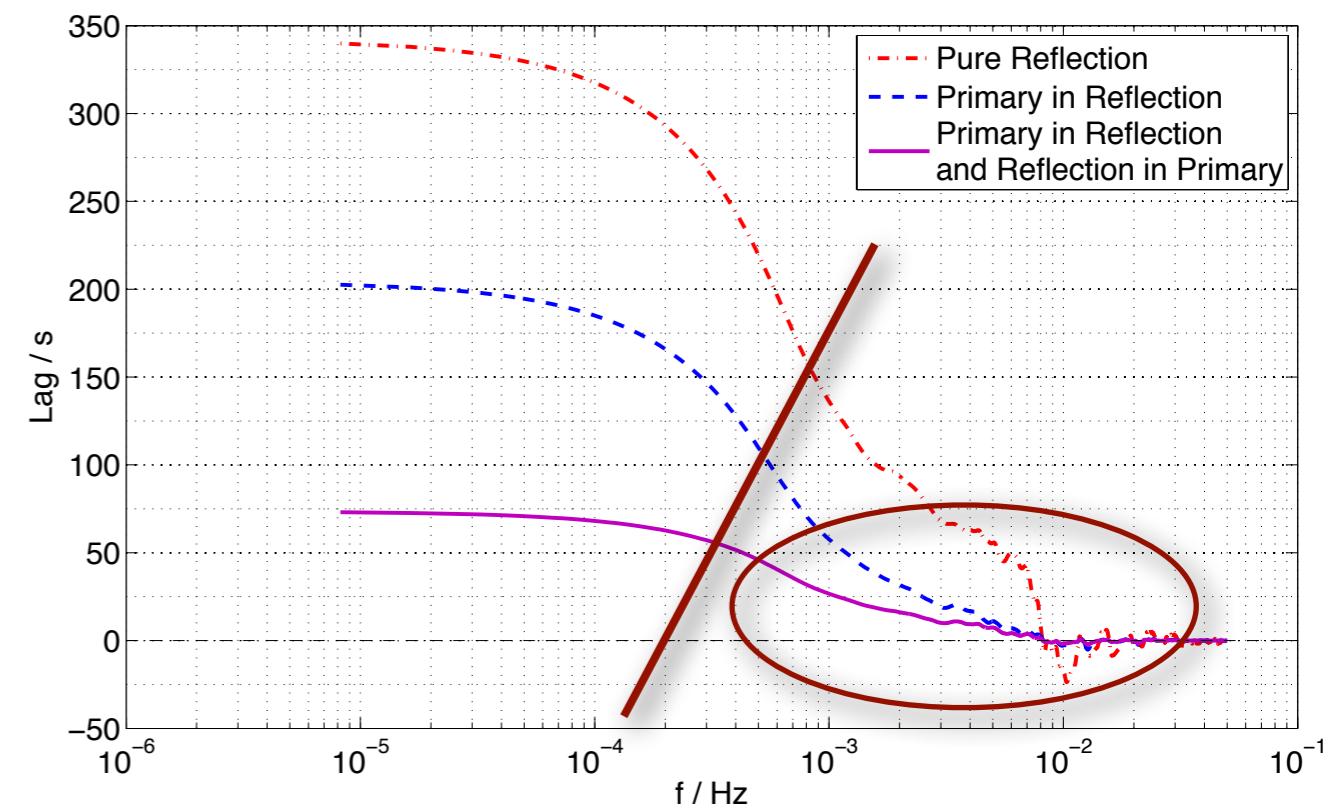
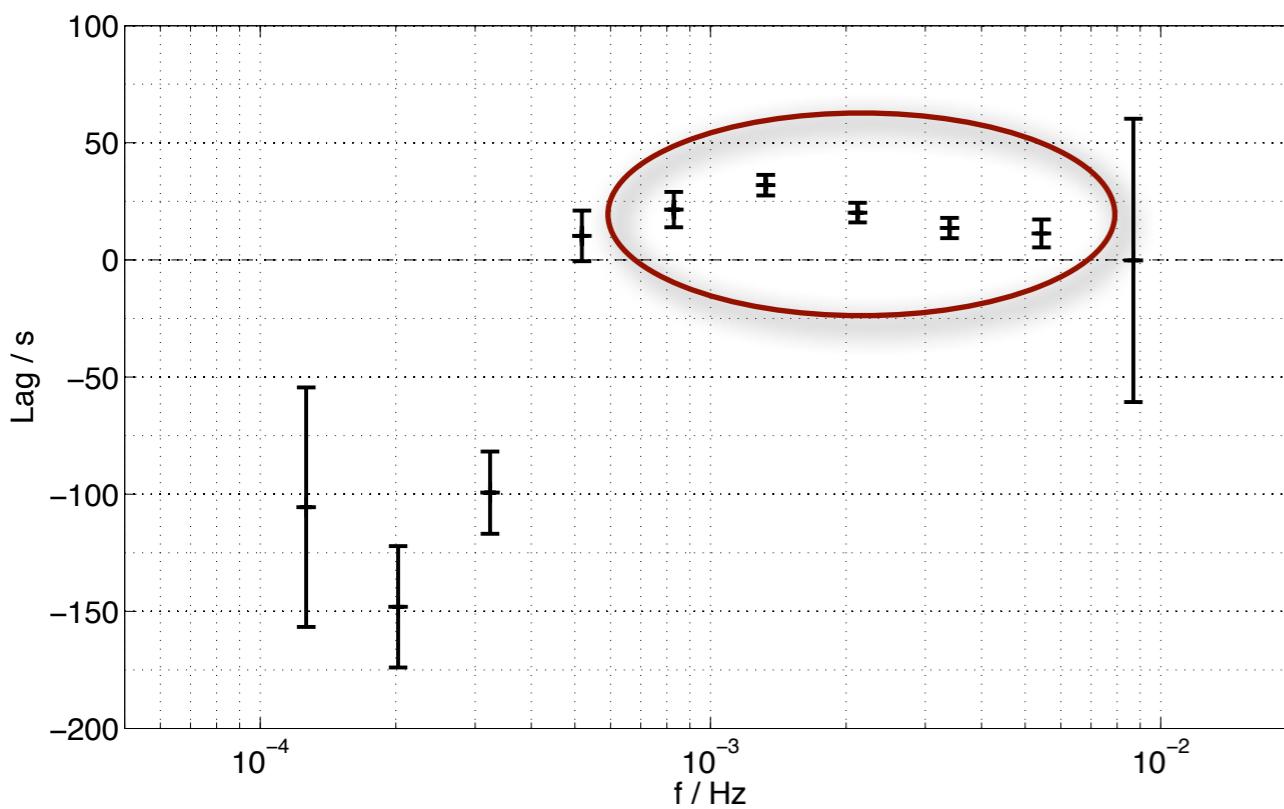
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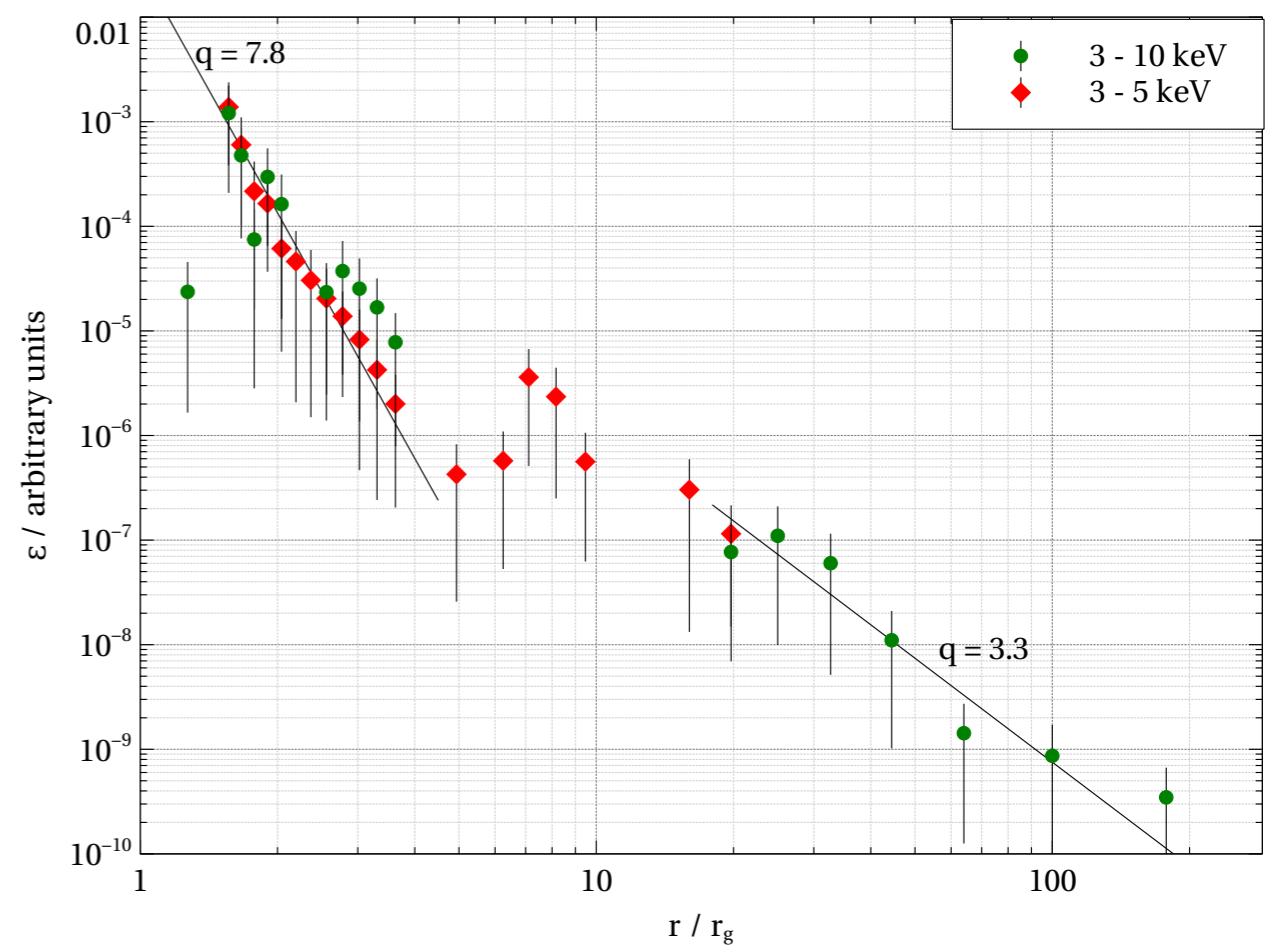
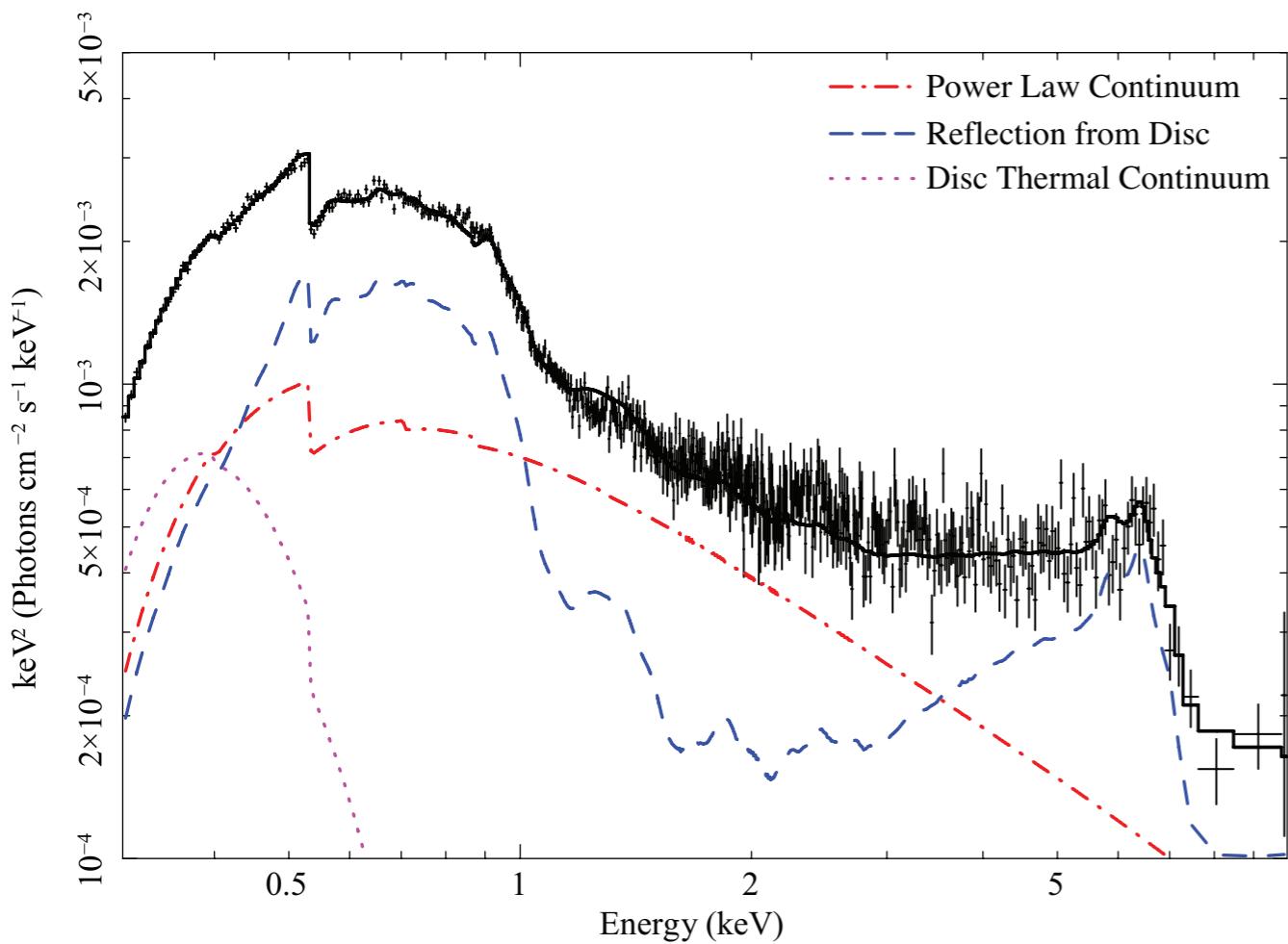
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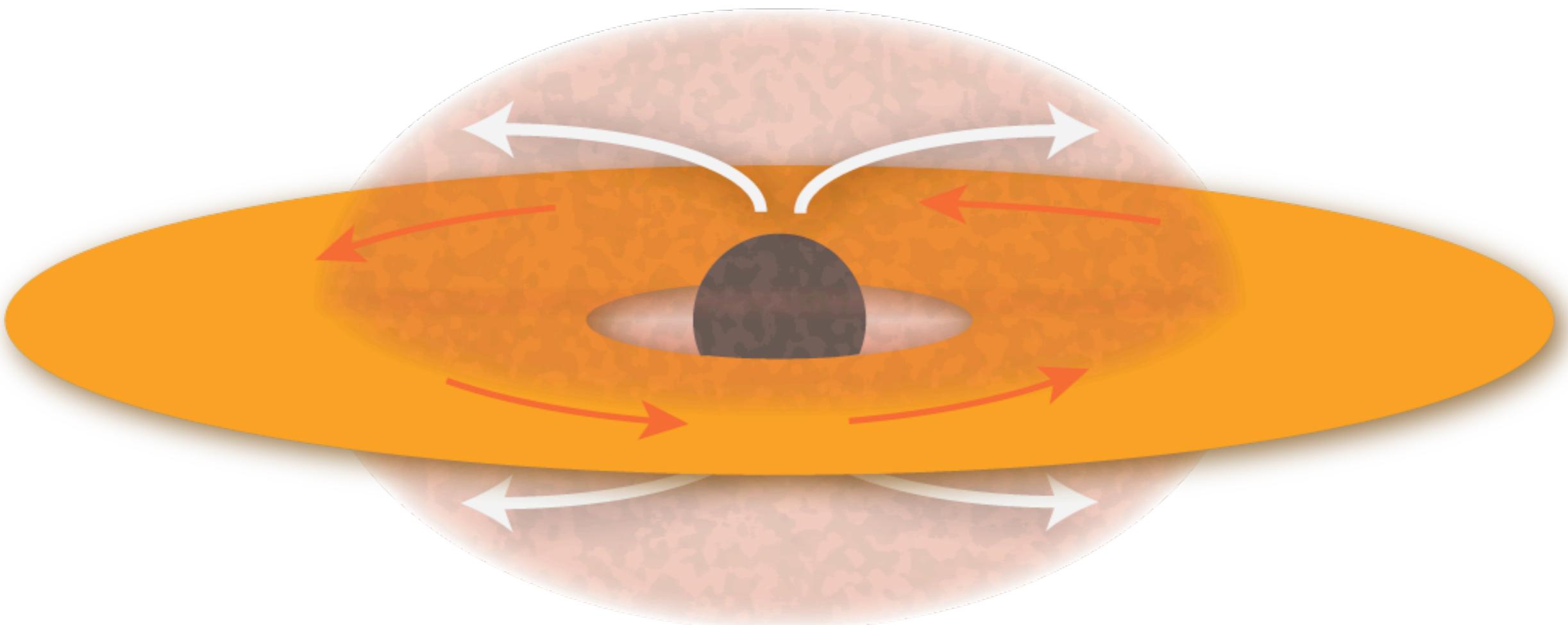
# Combined with the Spectrum...

Wilkins & Fabian 2011, 2012



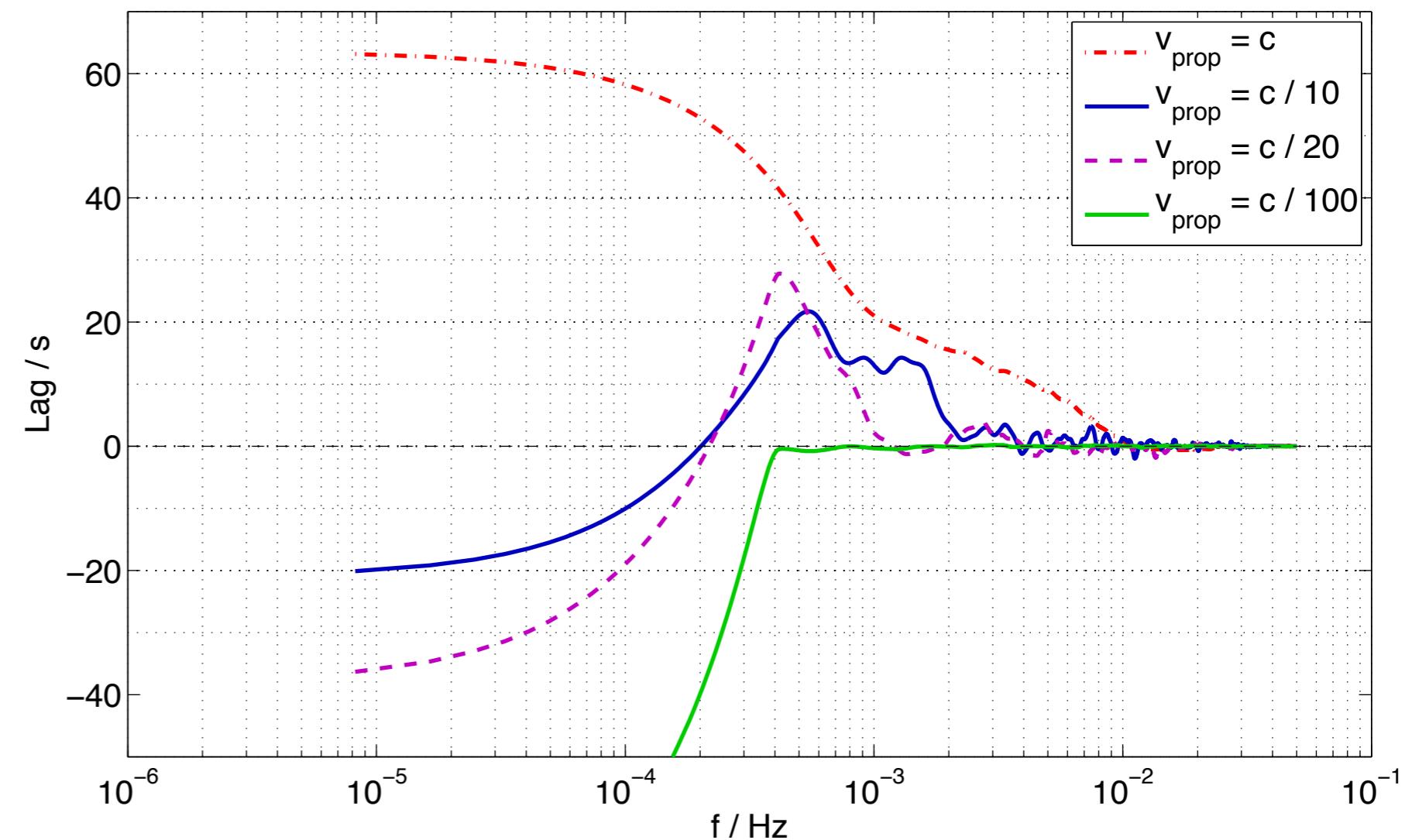
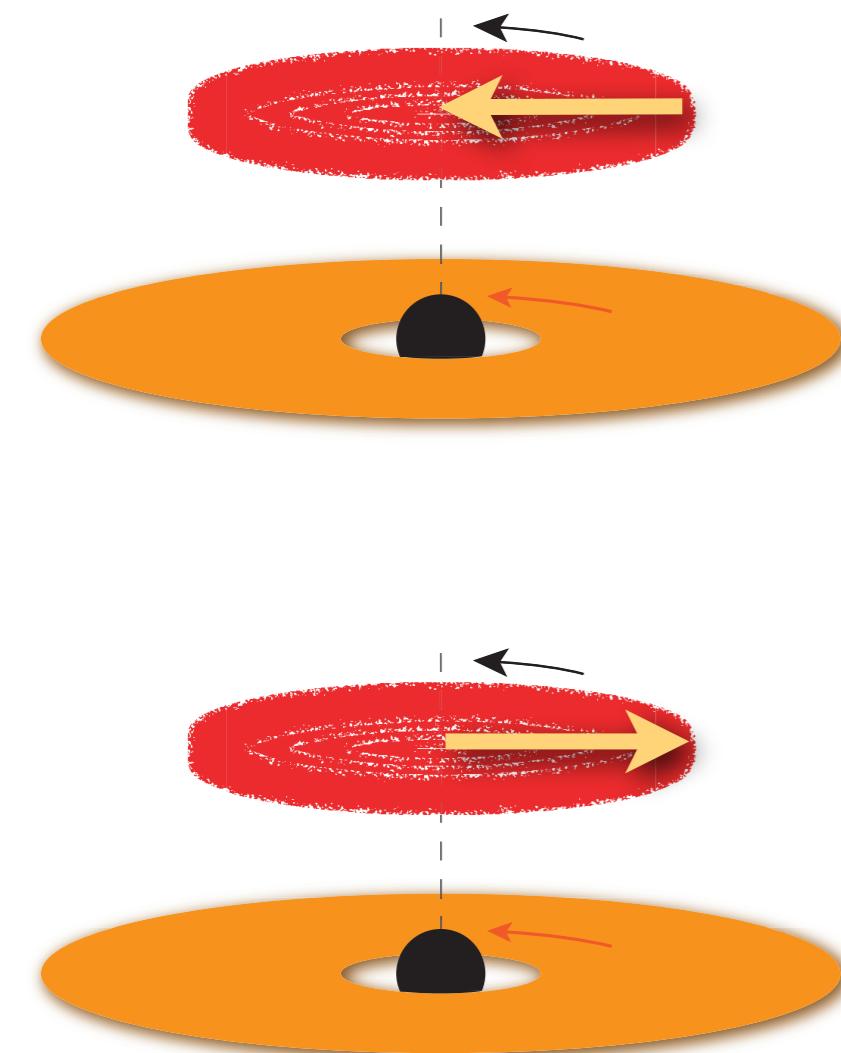
# ...we found the corona!

Wilkins & Fabian 2012, 2013



# Propagation Effects

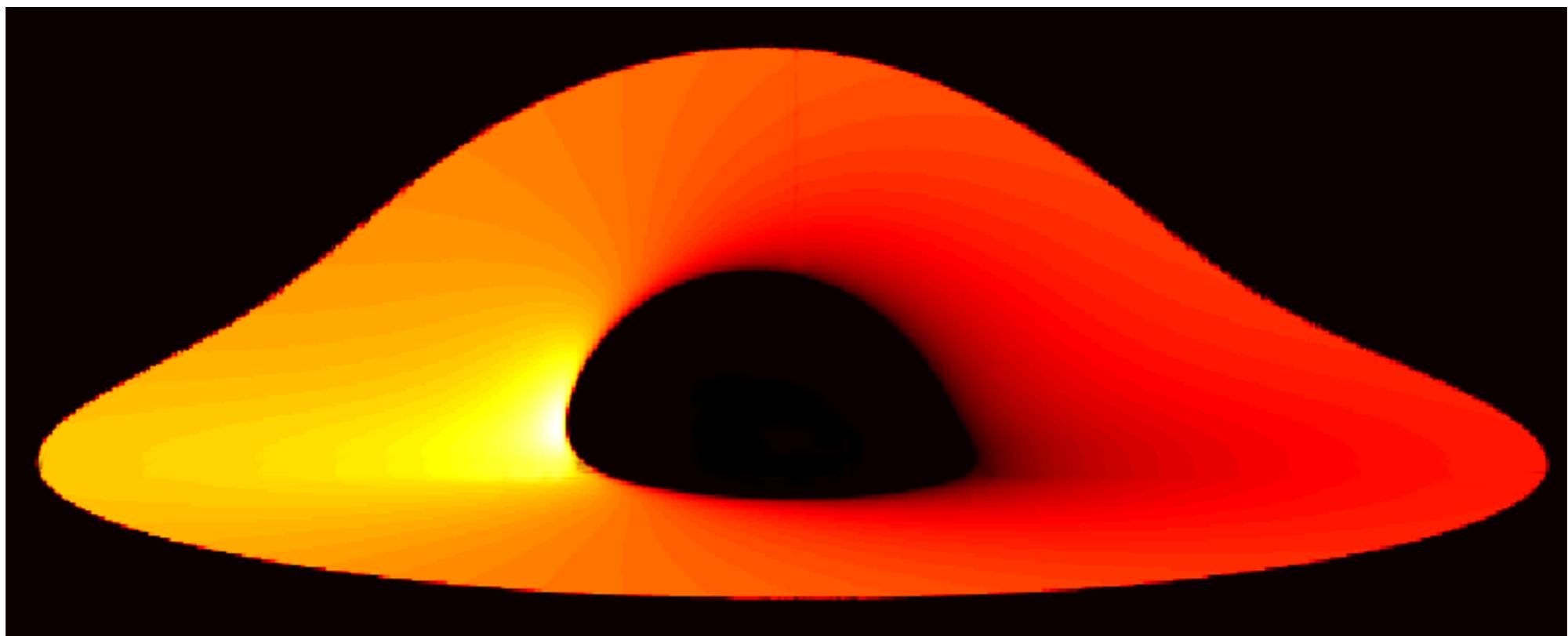
Wilkins & Fabian 2013, Arévalo & Uttley 2006



# Can we do better?

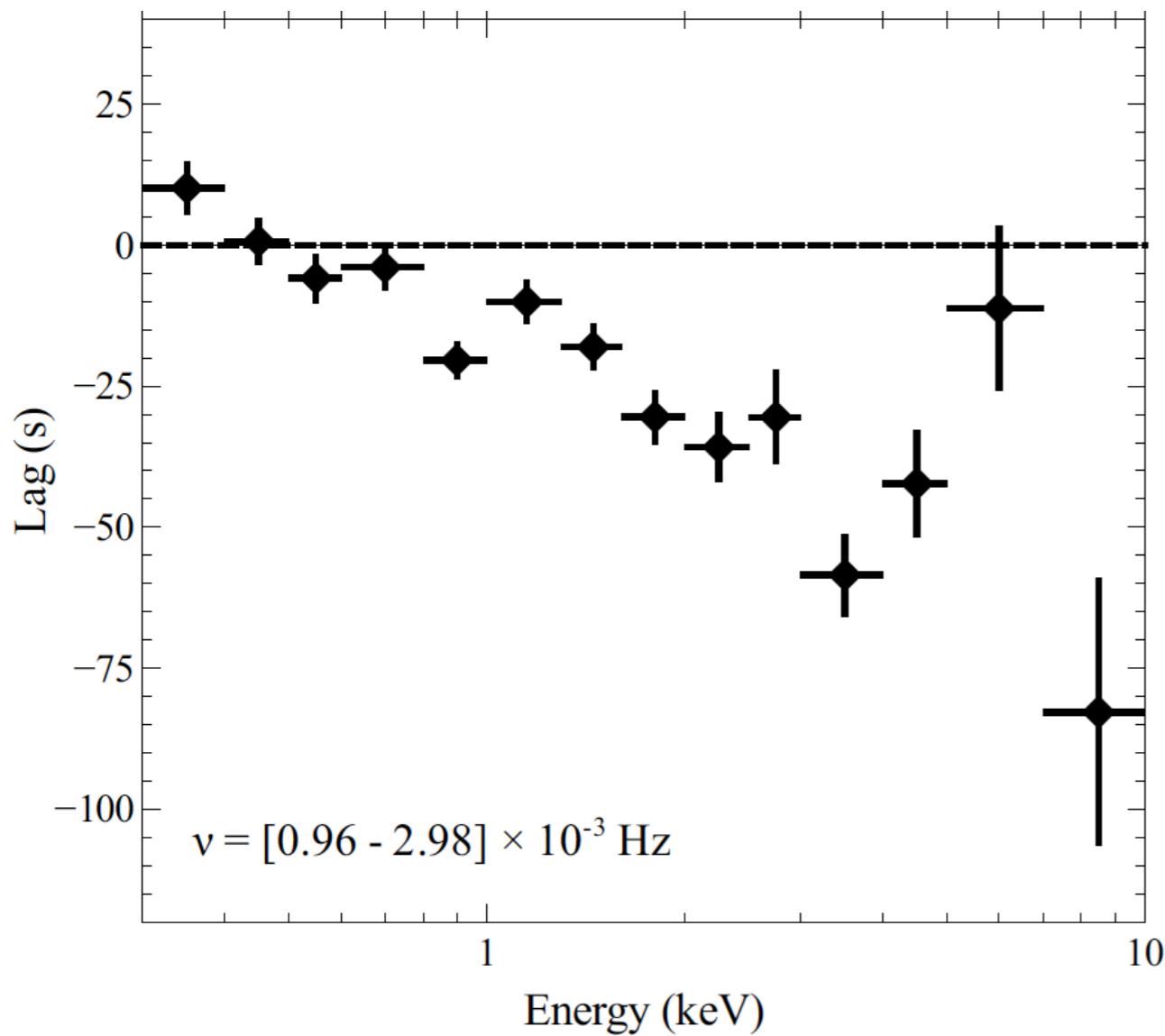
- Treated the energy spectrum and variability/reverberation separately
  - Signal to noise
  - They are predicted by the same model
  - Should be able to fit them simultaneously!
  - Better constraints on models rather than iterative best fitting between data sets
  - Breaks degeneracies

# Lags should be energy dependent



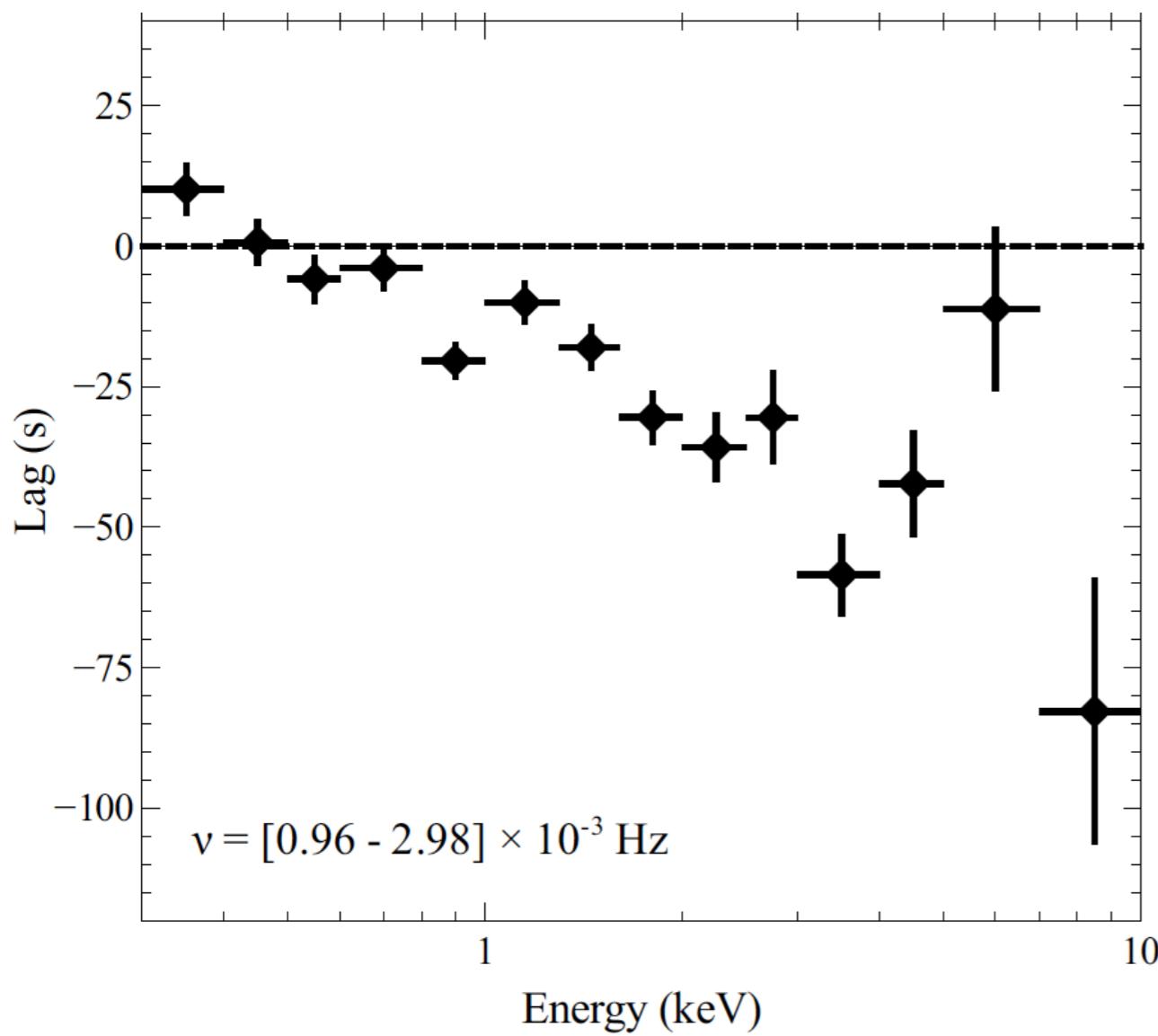
# The Lag/Energy Spectrum

Kara+2012

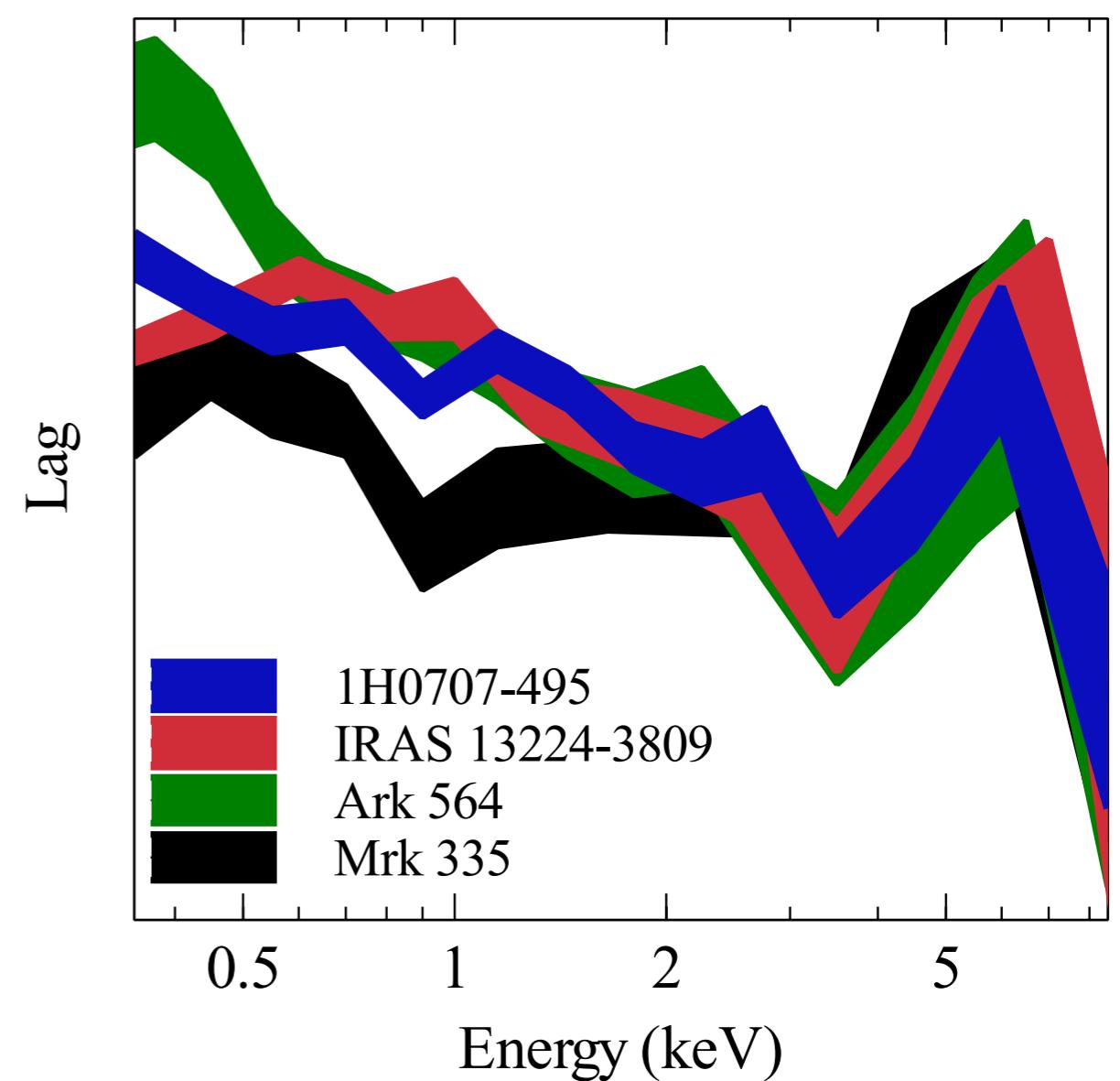


# The Lag/Energy Spectrum

Kara+2012

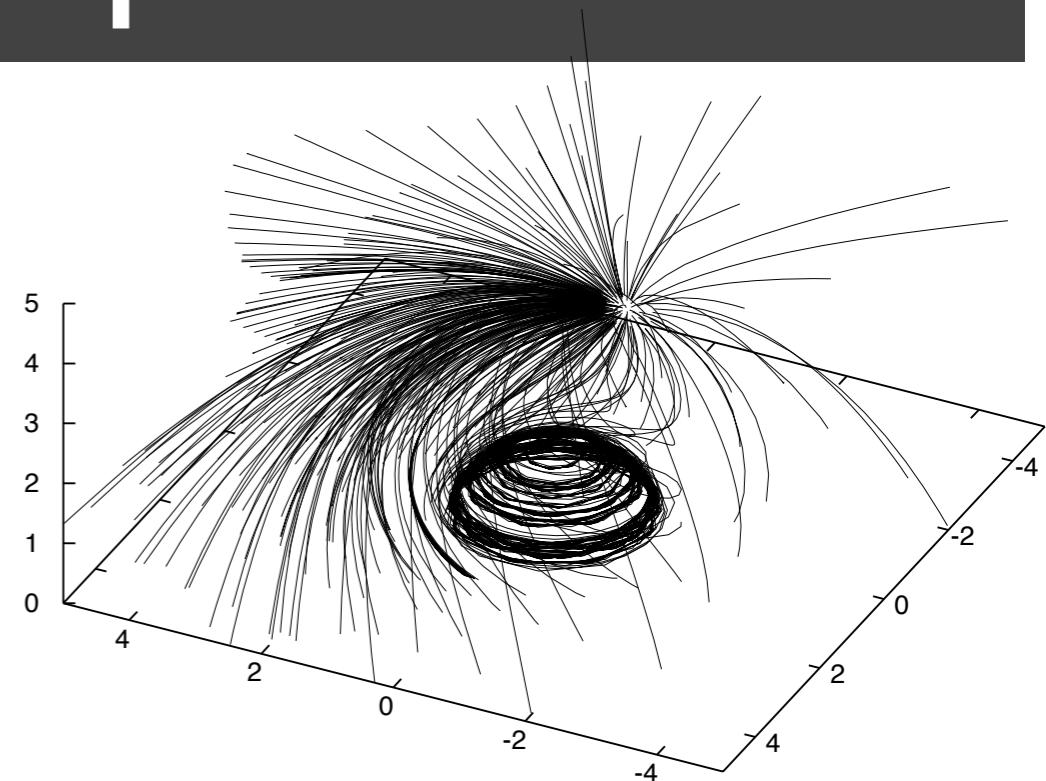


Kara+2013c

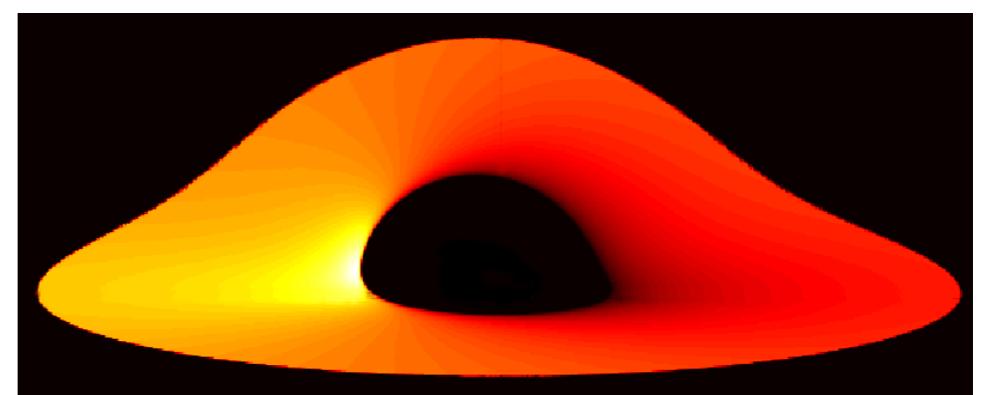


# Predicting Lag-Energy Spectra

- Trace rays from source to disc

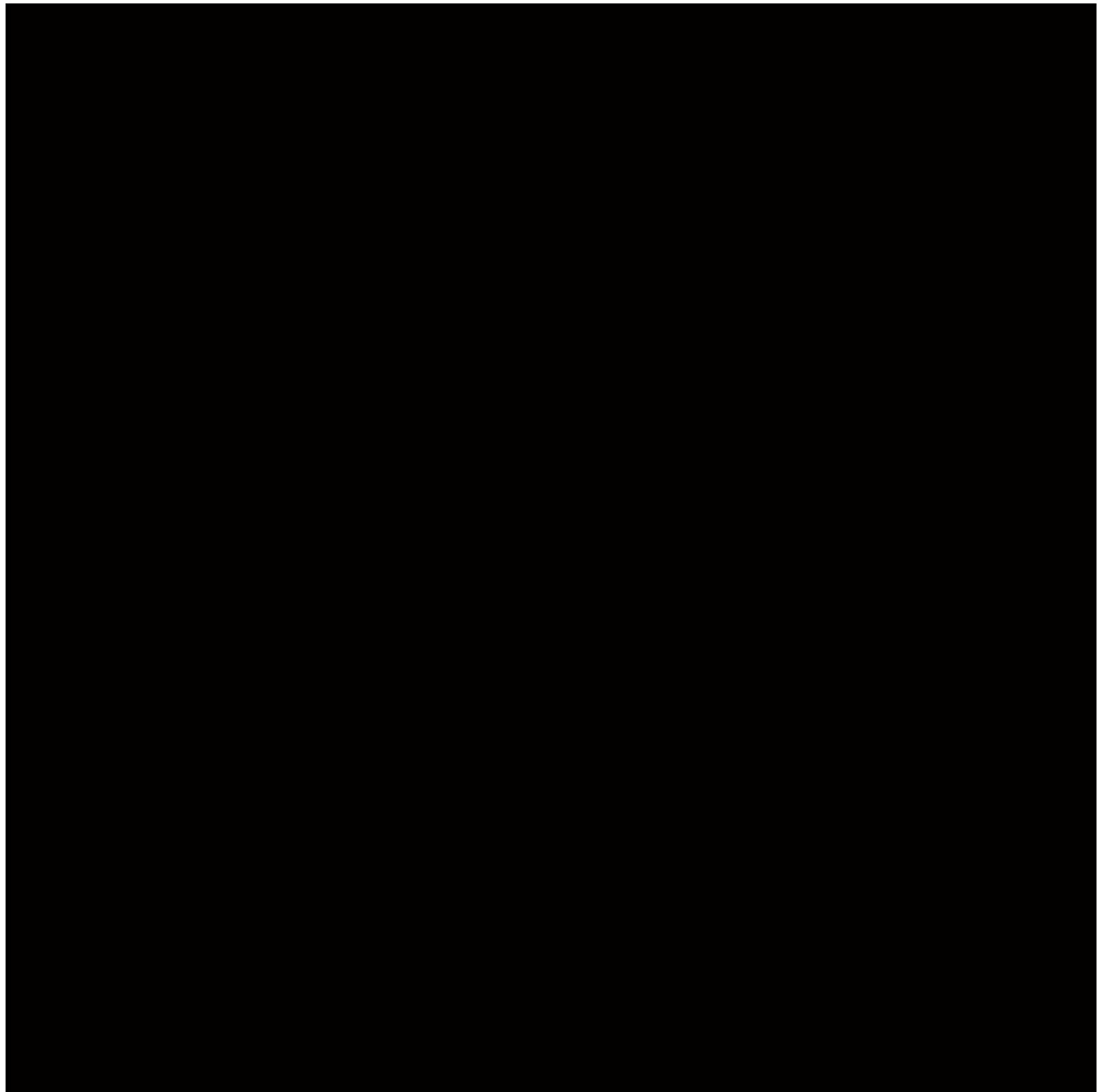


- Observe rays with telescope

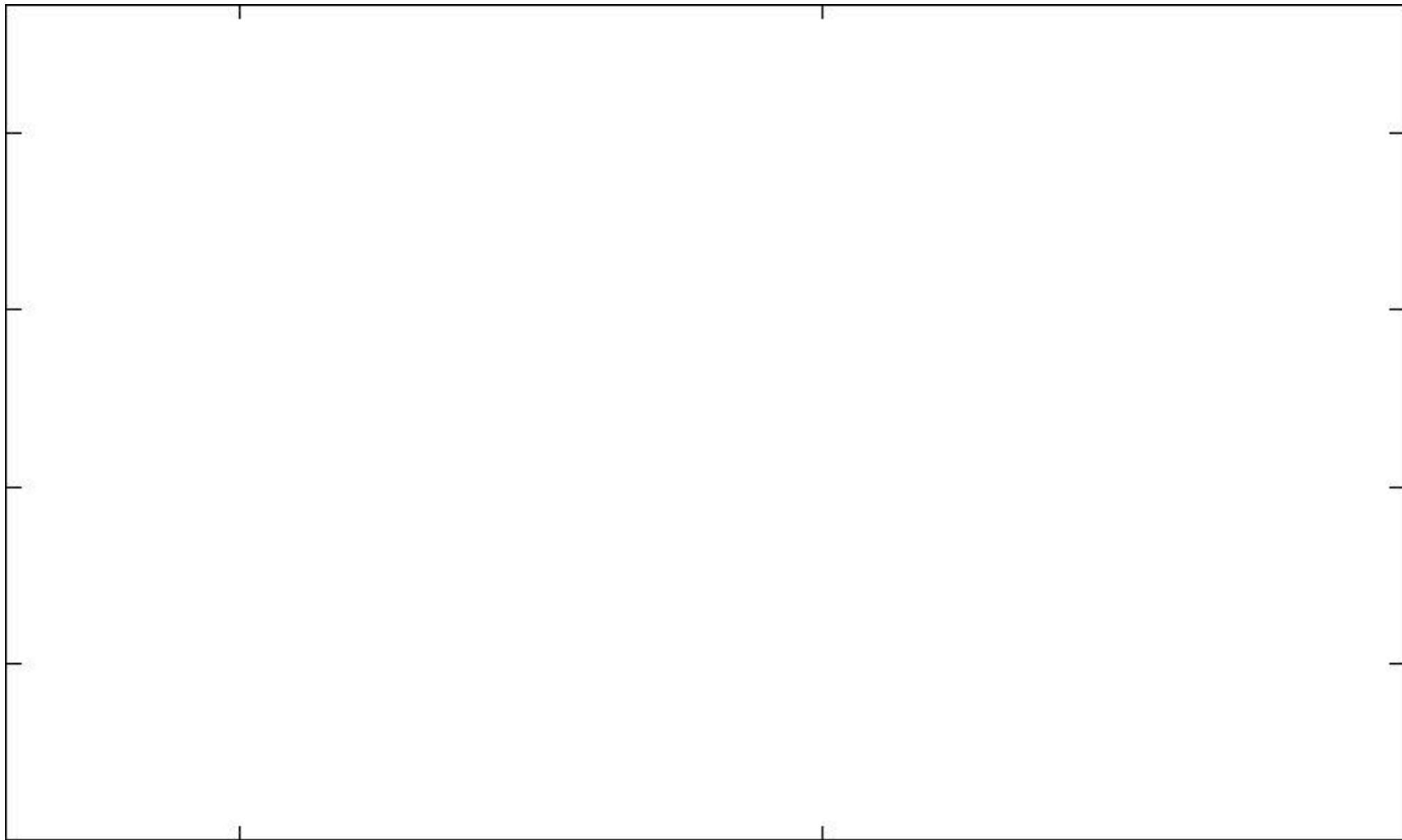


- For each, record its arrival time, redshift (energy) and intensity





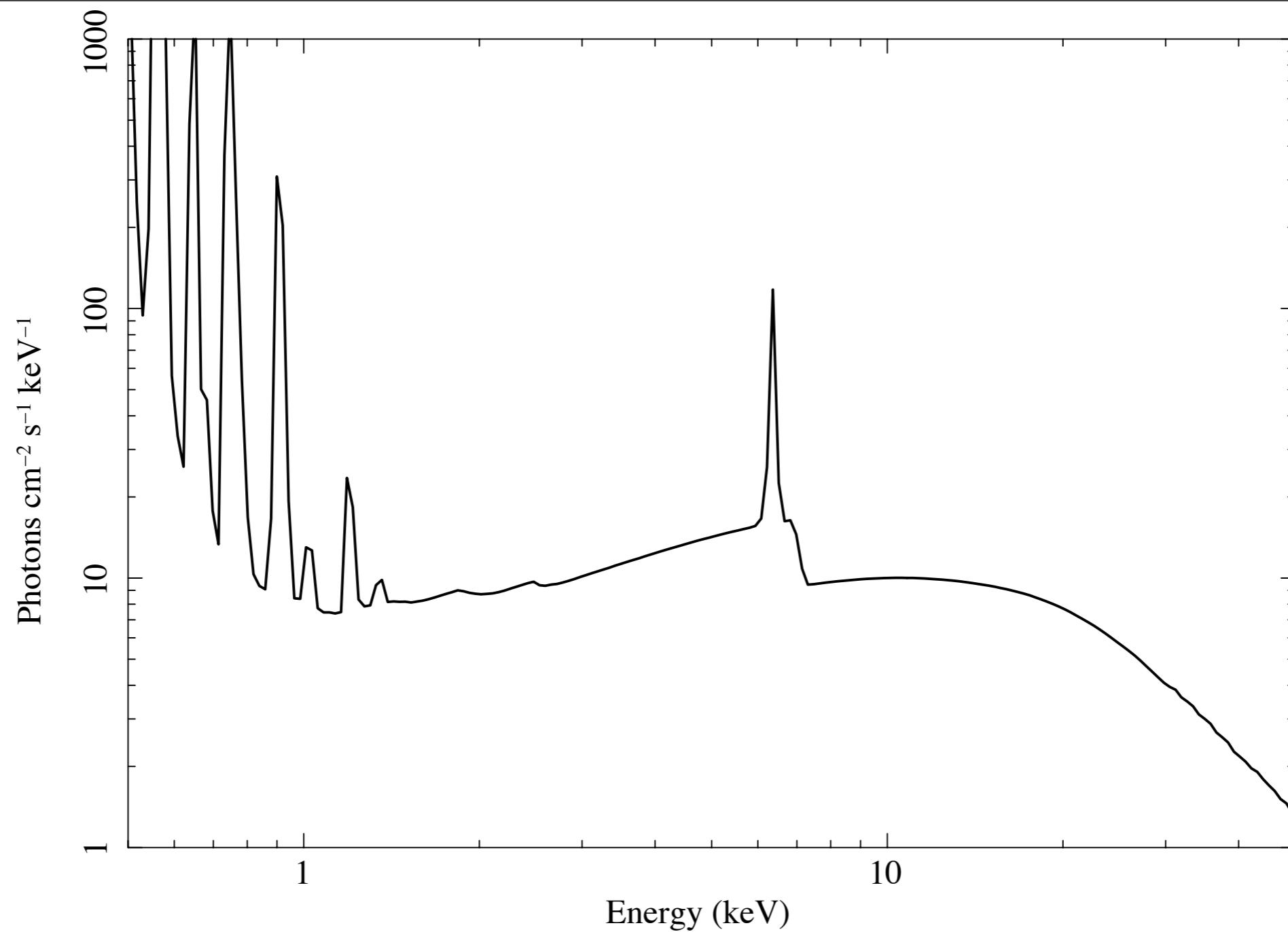




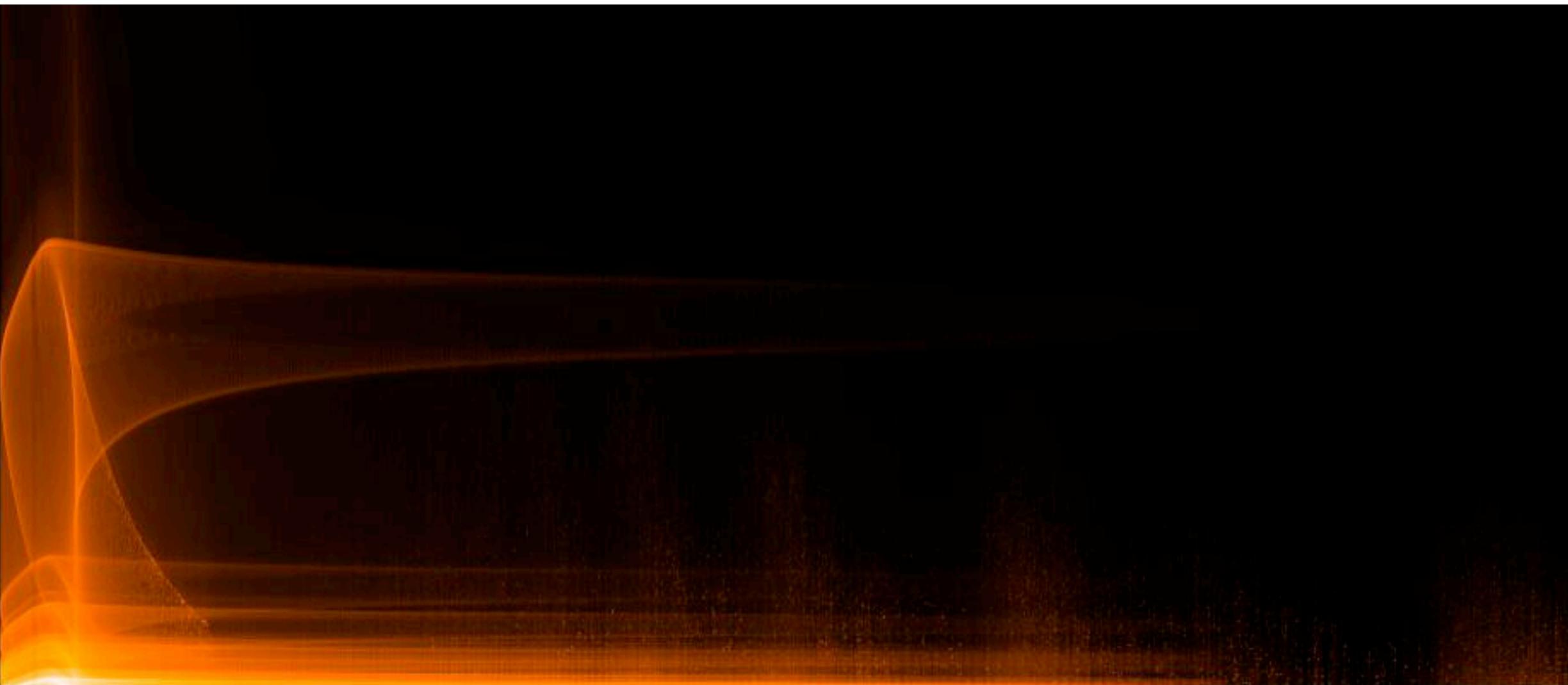
# The Time-Energy Transfer Function



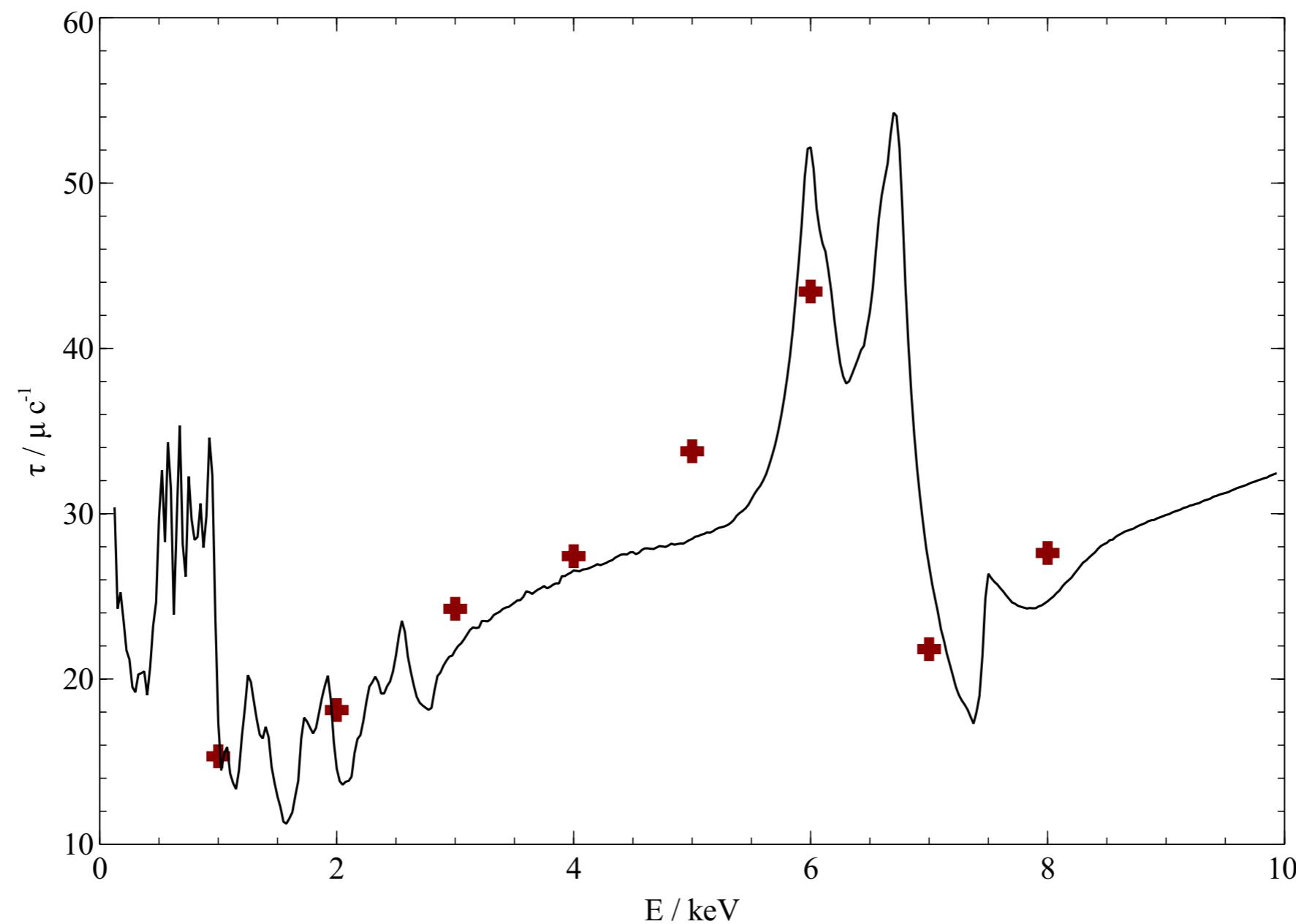
# The Reflection Spectrum



# Time-Resolved Reflection



# Lag/Energy Spectrum vI

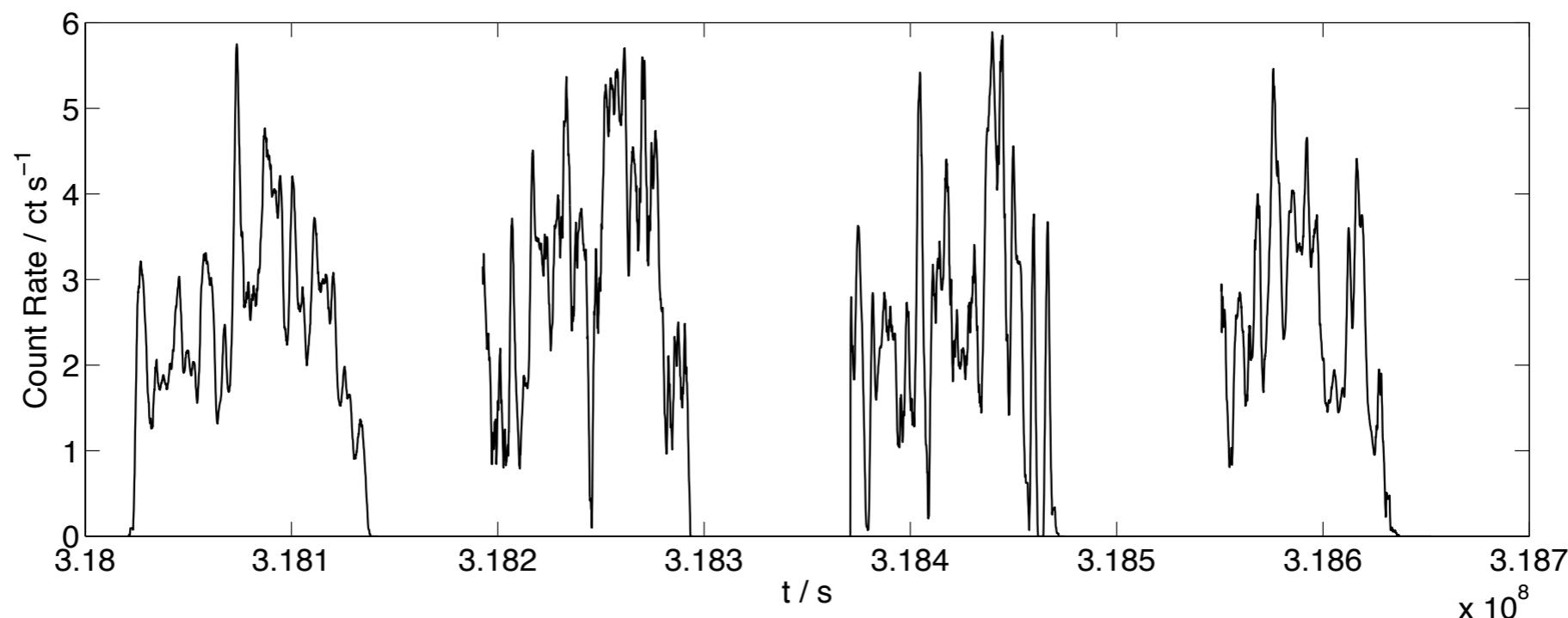


# The Fourier Transform

$$F(t) = \int \tilde{F}(\omega) e^{i\omega t} d\omega$$

$$\tilde{F}(\omega) = \int F(t) e^{-i\omega t} dt$$

$$\tilde{F}(\omega) = |\tilde{F}(\omega)| e^{i\varphi}$$



# The Lag Spectrum

$$\tilde{H}(\omega) = |\tilde{H}(\omega)| e^{i\varphi}$$

$$\tilde{S}(\omega) = |\tilde{S}(\omega)| e^{i\theta}$$

# The Lag Spectrum

$$\tilde{H}(\omega) = |\tilde{H}(\omega)| e^{i\varphi}$$

$$\tilde{S}(\omega) = |\tilde{S}(\omega)| e^{i\theta}$$

$$C = S^* H = |\tilde{S}| |\tilde{H}| e^{i(\varphi - \theta)}$$

# The Lag Spectrum

$$\tilde{H}(\omega) = |\tilde{H}(\omega)| e^{i\varphi}$$

$$S(t) = H(t) \otimes T(t)$$

$$\tilde{S}(\omega) = |\tilde{S}(\omega)| e^{i\theta}$$

$$\tilde{S}(\omega) = \tilde{H}(\omega)\tilde{T}(\omega)$$

$$C = S^* H = |\tilde{S}| |\tilde{H}| e^{i(\varphi-\theta)}$$

$$\tilde{C}(\omega) = |\tilde{H}|^2 |\tilde{T}| e^{i\varphi_T}$$

# The Lag Spectrum

$$\tilde{H}(\omega) = |\tilde{H}(\omega)| e^{i\varphi}$$

$$S(t) = H(t) \otimes T(t)$$

$$\tilde{S}(\omega) = |\tilde{S}(\omega)| e^{i\theta}$$

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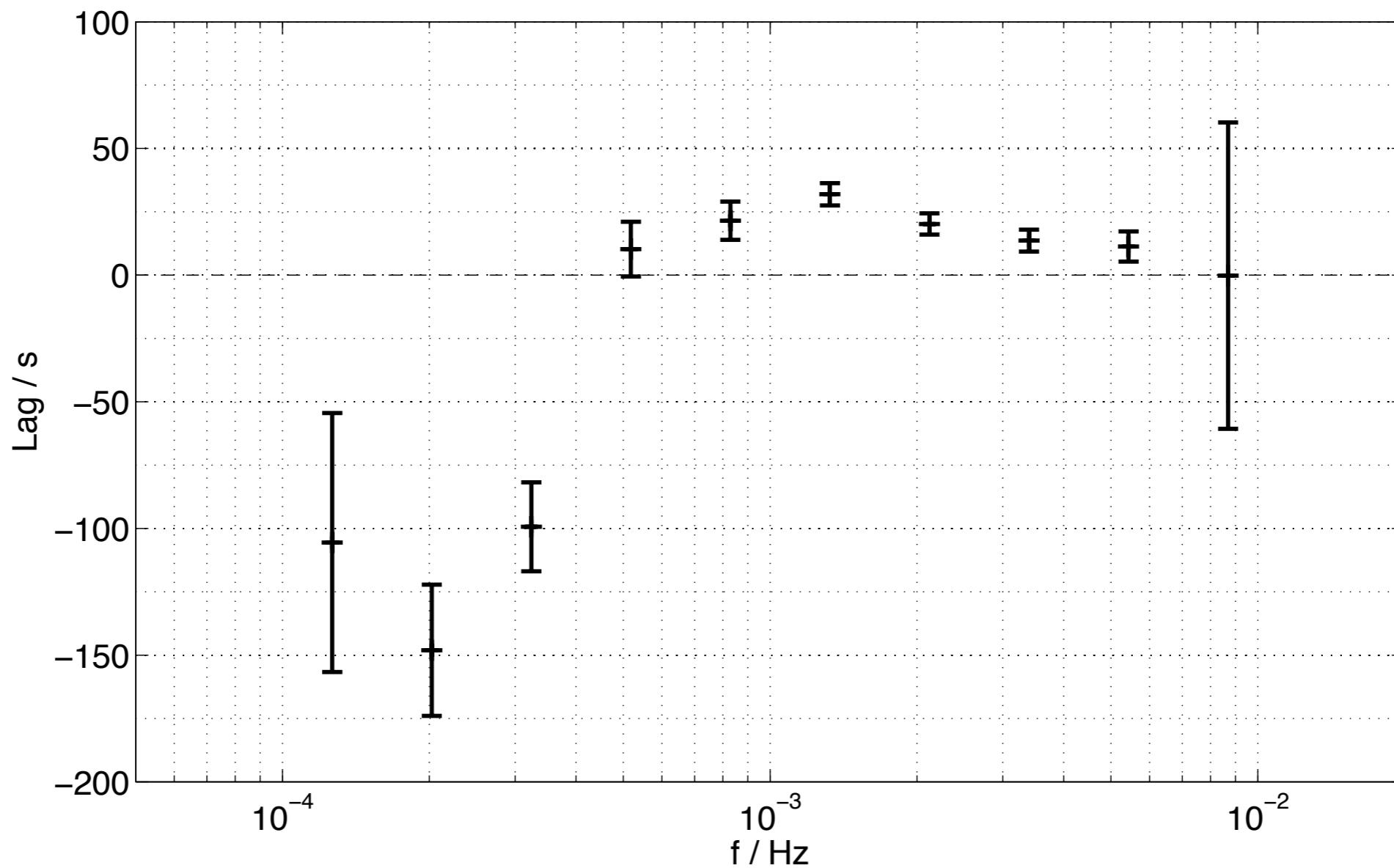
$$C = S^* H = |\tilde{S}| |\tilde{H}| e^{i(\varphi-\theta)}$$

$$\tilde{C}(\omega) = |\tilde{H}|^2 |\tilde{T}| e^{i\varphi_T}$$

$$\varphi = \omega t$$

$$\therefore \tau(\nu) = \frac{\arg(C(\nu))}{2\pi\nu}$$

# Lag/Frequency Spectrum



# Lag/Energy/Frequency Spectrum



# The Reference Band

- Intrinsic variability of the source,  $S(t)$
- Each energy band has its own transfer function

$$L_1(t) = S(t) \otimes T_1(t)$$

$$L_2(t) = S(t) \otimes T_2(t)$$

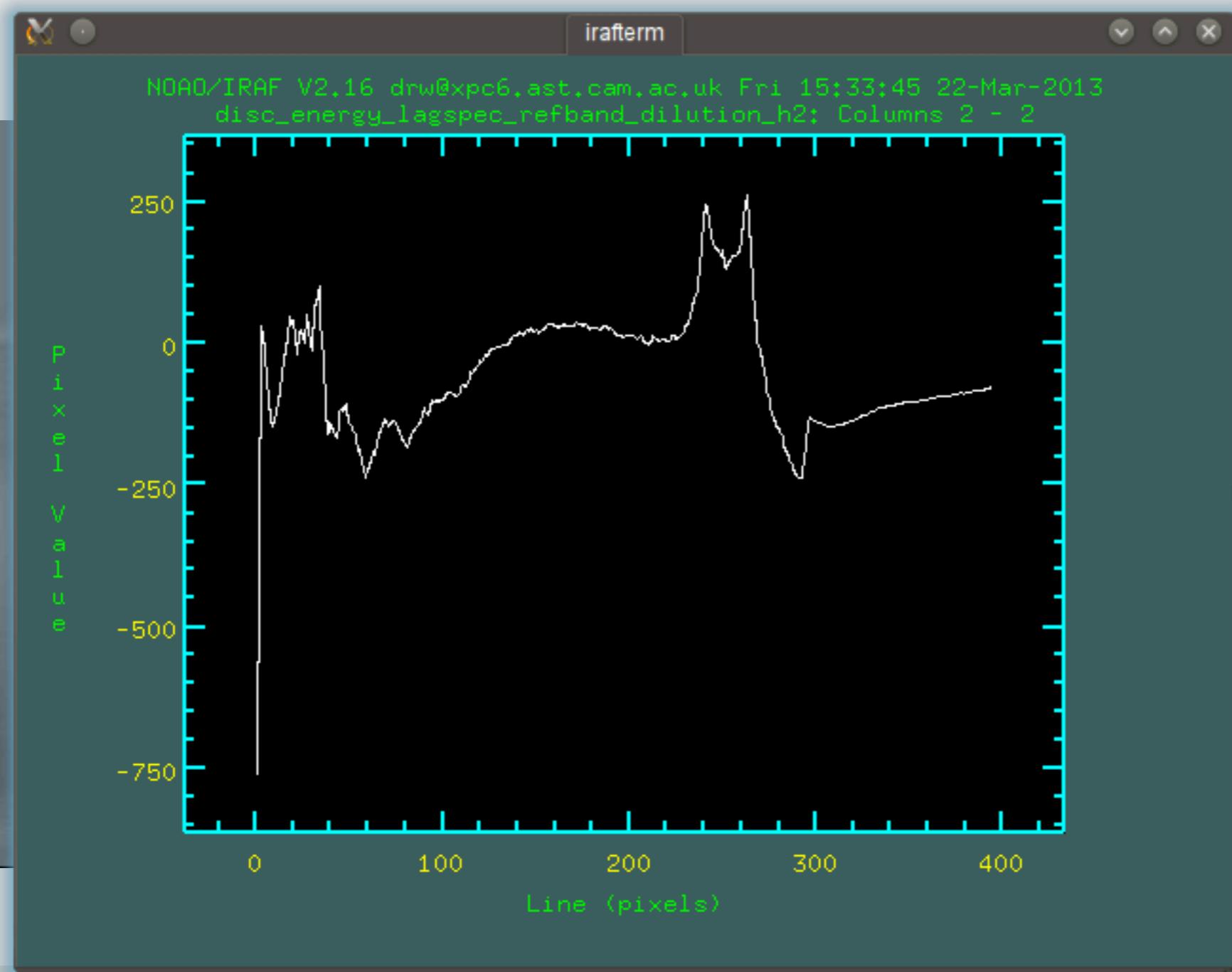
- Giving the cross spectrum

$$\tilde{C} = \tilde{L}_2^* \tilde{L}_1 = |\tilde{S}|^2 \tilde{T}_2^* \tilde{T}_1$$

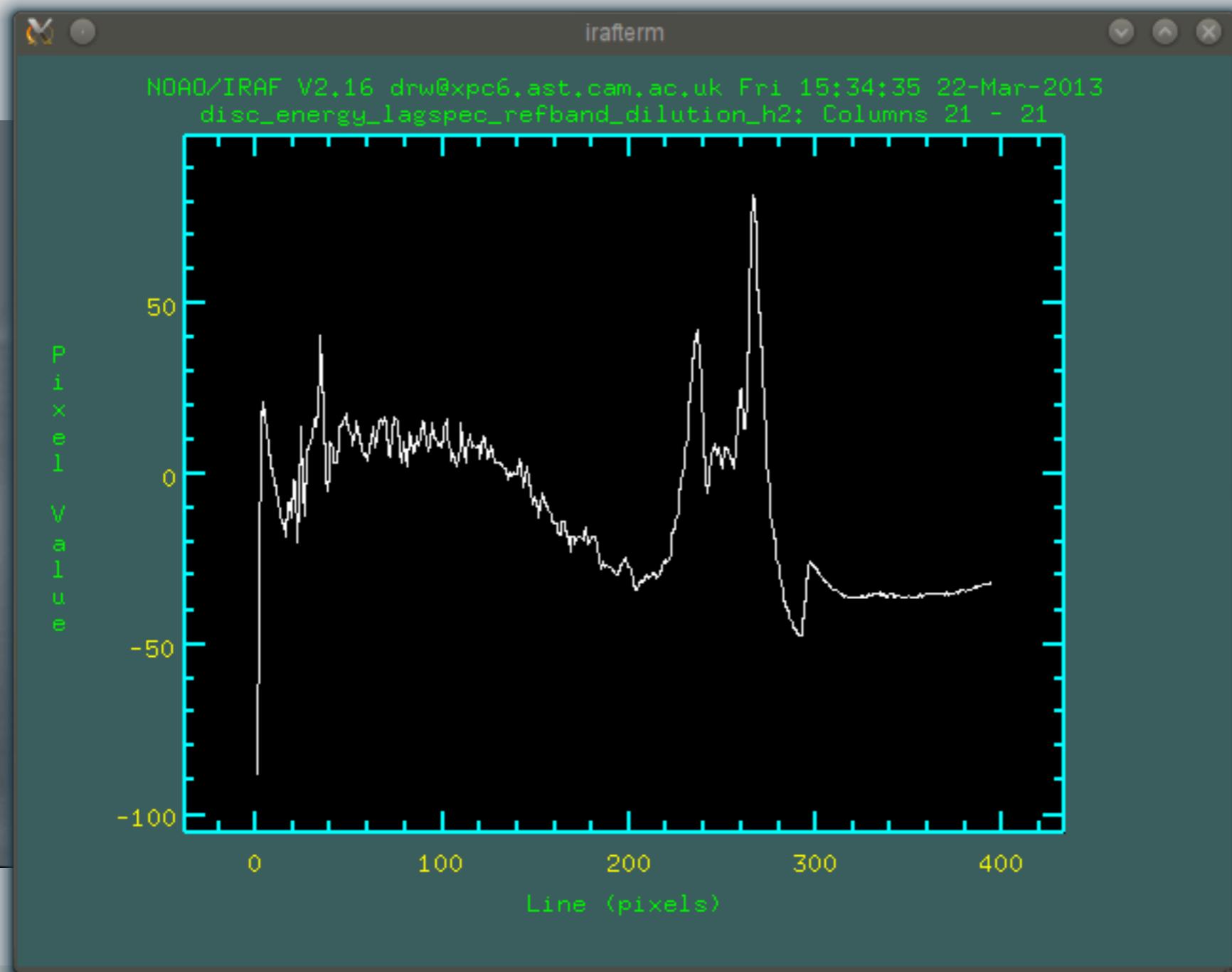
# Lag/Energy/Frequency Spectrum



# Lag/Energy/Frequency Spectrum



# Lag/Energy/Frequency Spectrum



# The Current State of Affairs

- Limited by number of counts and uncorrelated noise
- Limits energy and frequency resolution



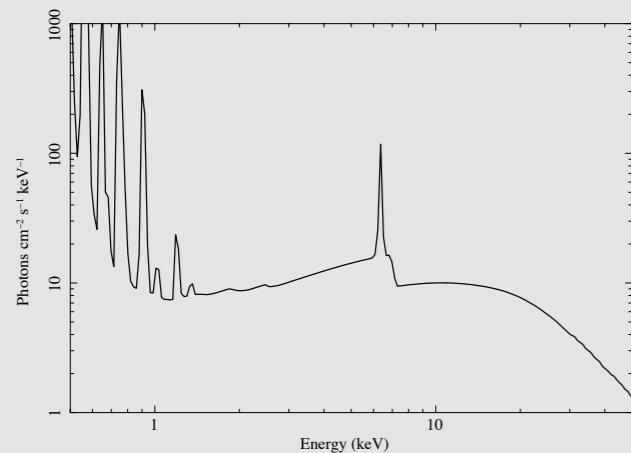
- Also lose the low energy part to the hard lag

# Model

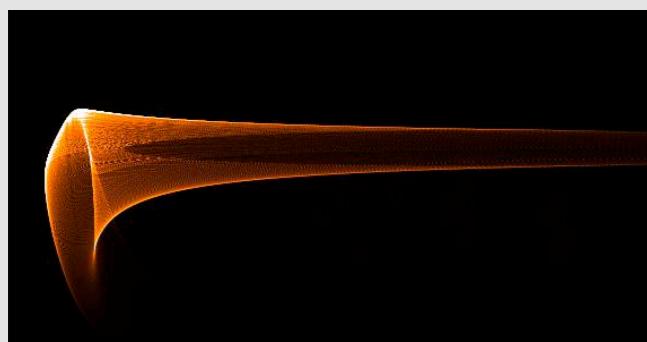
powerlaw

+

reflionx



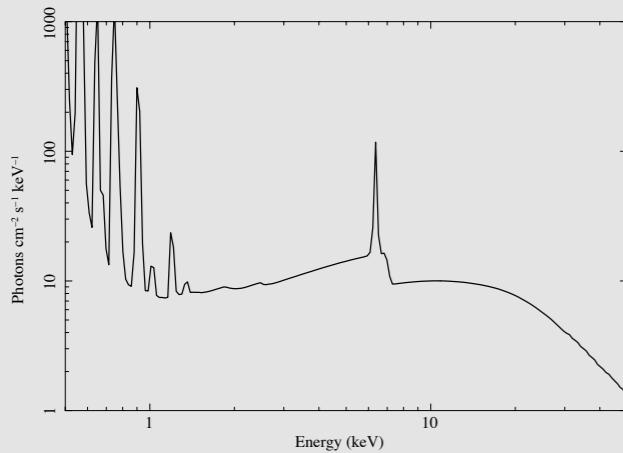
Disc Response



Model  
powerlaw

+

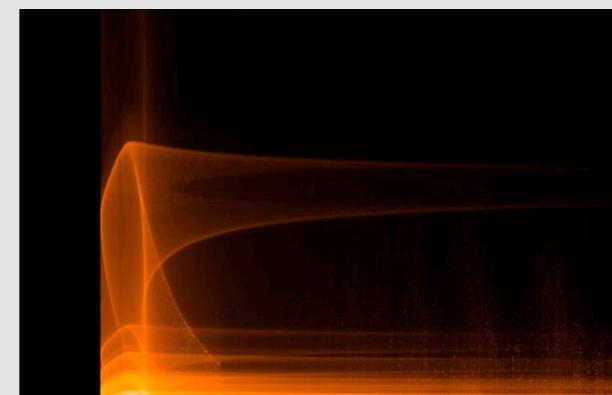
reflionx



⊗  
Disc Response



# Instrument Response



\*

ARF

⊗

RMF

⊗

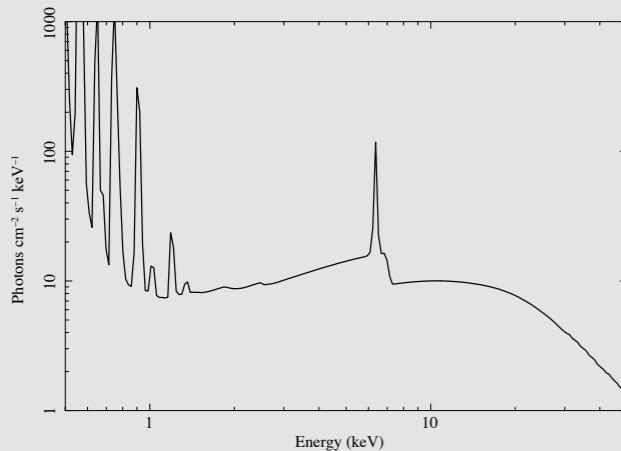
Timing Response

# Model

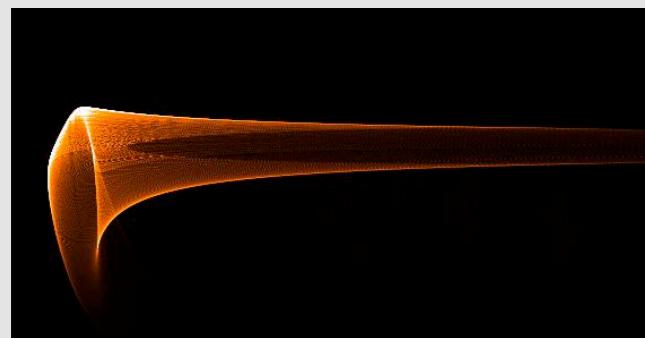
powerlaw

+

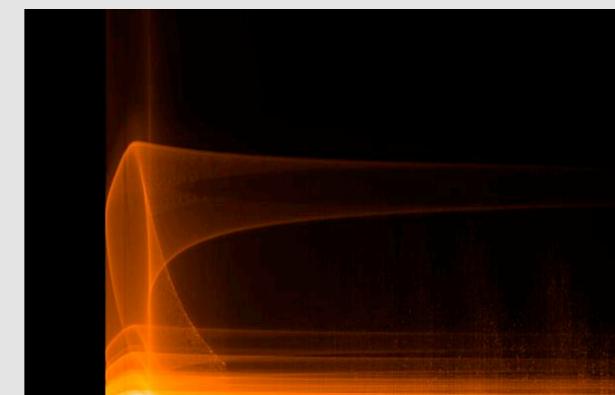
reflionx



 Disc Response



# Instrument Response



\*

ARF



RMF



Timing Response

# Cross Spectrum

## Fourier Transform

$$\tilde{C} = \tilde{L}_2^* \tilde{L}_1 = |\tilde{S}|^2 \tilde{T}_2^* \tilde{T}_1$$

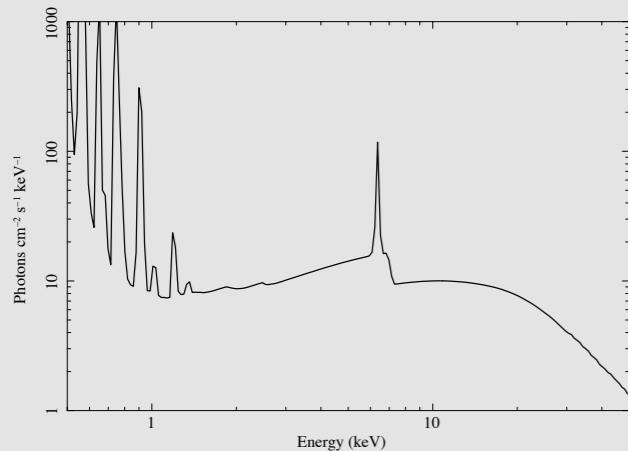
Fit to data (E, ν)

# Model

powerlaw

+

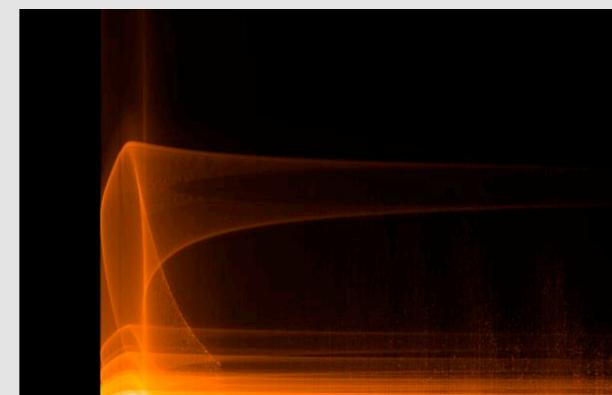
reflionx



$\otimes$   
Disc Response



# Instrument Response



\*

ARF



RMF



Timing Response

# Cross Spectrum

## Fourier Transform

$$\tilde{C} = \tilde{L}_2^* \tilde{L}_1 = |\tilde{S}|^2 \tilde{T}_2^* \tilde{T}_1$$

Fit to data ( $E, \nu$ )

# Lag Spectra

$$T(\nu) = \frac{\arg C(\nu)}{2\pi\nu}$$

# Conclusions

- Predicting lag/energy/frequency spectra for X-ray reverberation models from ray tracing simulations
- Need to understand what we are measuring and its frequency and energy dependence
- Can construct spectra from combinations of energy, (lag) time, frequency and counts
- Models must simultaneously fit all of these spectra